

Mathletics

Series



Teacher



$\frac{12}{20}$ $\frac{16}{48}$ $\frac{1}{2}$ $\frac{2}{4}$ $\frac{6}{12}$ $\frac{75}{150}$ $\frac{3455}{6910}$
89.021 312.956

Fractions, Decimals and Percentages



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Series G – Fractions, Decimals and Percentages

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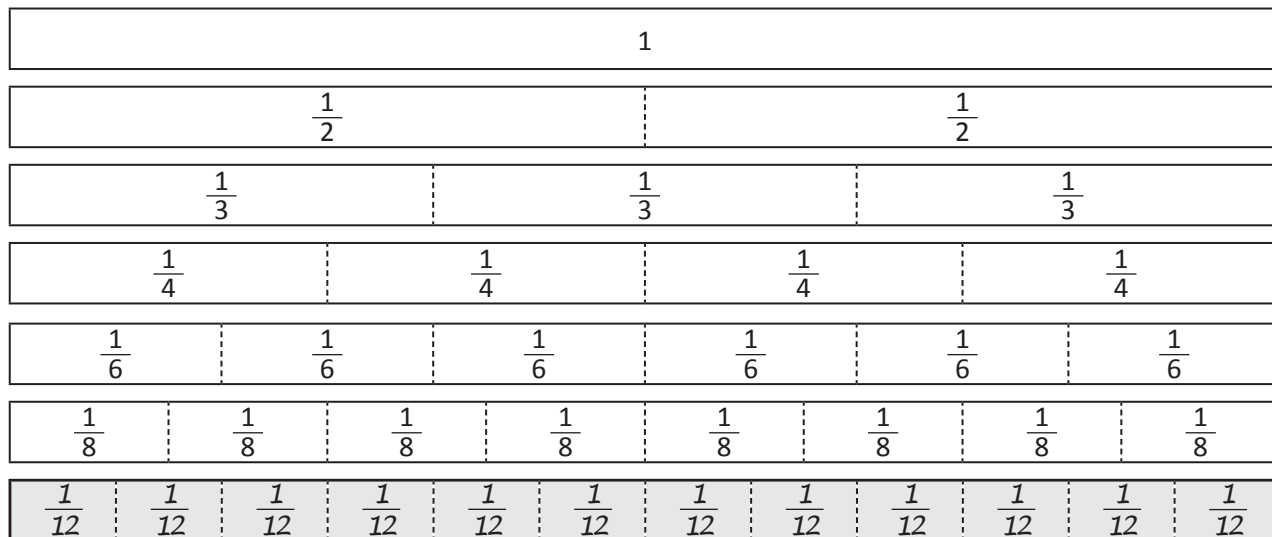
Series Authors:

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Nicola Herringer

Fractions – equivalent fractions

Equivalent fractions have the same value but they have different denominators.
This means they have been divided into a different number of parts.



1 Use the wall to find the equivalent fractions:

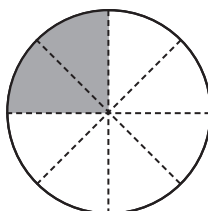
- a What fractions can you find that are equivalent to $\frac{2}{3}$? $\frac{4}{6}$
- b What fractions can you find that are equivalent to $\frac{3}{4}$? $\frac{6}{8}$
- c How many eighths are equivalent to $\frac{1}{2}$? 4
- d How many quarters are equivalent to $\frac{4}{8}$? 2
- e Divide the bottom row into twelfths. Find some equivalent fractions for $\frac{4}{12}$. $\frac{1}{3}, \frac{2}{6}$

2 Divide and shade the shapes to show the following equivalent fractions. The first one has been done for you.

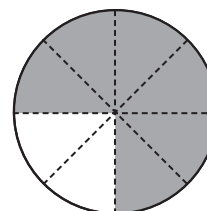
a $\frac{1}{2} = \frac{2}{4}$



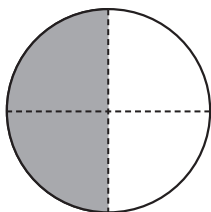
b $\frac{1}{4} = \frac{2}{8}$



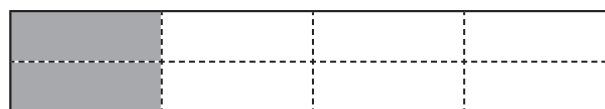
c $\frac{3}{4} = \frac{6}{8}$



d $\frac{1}{2} = \frac{2}{4}$



e $\frac{1}{4} = \frac{2}{8}$



Fractions – equivalent fractions

To find equivalent fractions without drawing diagrams we use the numerators and denominators to guide us.

Imagine your share of a cake is half. It is too big to pick up so you cut your half into halves. You now have 2 quarters of the cake.

You have doubled the number of parts (the denominator) and by doing this you have doubled the number of parts (the numerator).

This method can be used to find all equivalent fractions.

$$\frac{1}{2} = \frac{2}{4}$$

$\times 2$
 $\times 2$

3 Use the clues to help you make the equivalent fractions:

a $\frac{1}{3} = \frac{4}{12}$

$\times 4$
 $\times 4$

b $\frac{1}{2} = \frac{3}{6}$

$\times 3$
 $\times 3$

c $\frac{2}{3} = \frac{6}{9}$

$\times 3$
 $\times 3$

d $\frac{3}{8} = \frac{15}{40}$

$\times 5$
 $\times 5$

e $\frac{1}{3} = \frac{3}{9}$

f $\frac{1}{4} = \frac{2}{8}$

g $\frac{3}{4} = \frac{15}{20}$

h $\frac{2}{4} = \frac{1}{2}$

4 We can also reduce the number of parts in a whole. We divide to do this:

a $\frac{18}{24} = \frac{3}{4}$

$\div 6$
 $\div 6$

b $\frac{9}{21} = \frac{3}{7}$

$\div 3$
 $\div 3$

c $\frac{40}{48} = \frac{5}{6}$

$\div 8$
 $\div 8$

d $\frac{12}{18} = \frac{2}{3}$

e $\frac{12}{21} = \frac{4}{7}$

f $\frac{25}{40} = \frac{5}{8}$

Whatever we do to the top, we do to the bottom. Whatever we do to the bottom, we do to the top.



CHECK

5 Answer the following:

- a Cassie's table of kids won a pizza for having the most table points at the end of term. There are 6 kids at the table. What fraction of the pizza will they each receive?

$$\frac{1}{6}$$

- b The pizza has been cut into 12 pieces. How many slices does each kid get? 2

What is this as a fraction?

$$\frac{2}{12}$$

- c Stavros reckons that because they got 2 slices they got more than they would have if the pizza had been cut into 6 pieces. Is he right? Explain your answer with words or diagrams.

No. It's the same. $\frac{2}{12} = \frac{1}{6}$

Fractions – mixed numerals and improper fractions

Mixed numerals are made up of whole numbers and fractions.

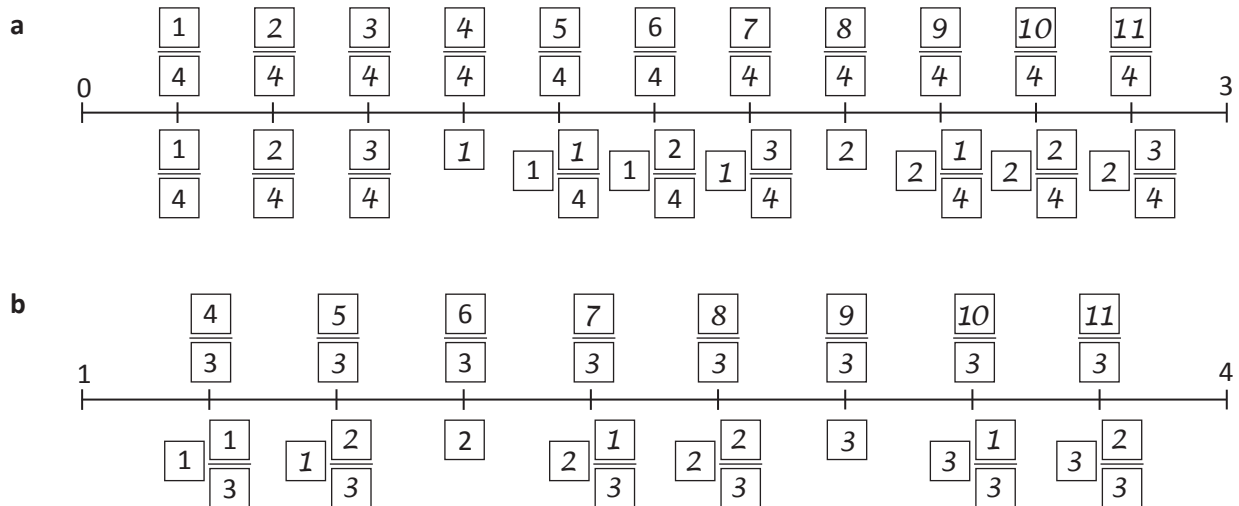
$2\frac{1}{2}$ is a mixed number.

Mixed numbers can also be expressed as improper fractions.

$2\frac{1}{2}$ can also be written as $\frac{5}{2}$.



1 Complete the number lines by filling in the boxes:



2 Use the number lines above to help you find the mystery fractions. Score 5 points for a correct answer. Lose 3 points for a wrong answer. For some questions, more than 1 answer is correct. The first one has been done for you.

My score

Q1 This improper fraction is equivalent to 2.

A1 $\frac{6}{3}$ or $\frac{8}{4}$

Q2 This improper fraction comes directly before $1\frac{2}{4}$.

A2 $\frac{5}{4}$

Q3 This improper fraction is one third greater than $3\frac{1}{3}$.

A3 $\frac{11}{3}$

Q4 This mixed numeral is the same as $\frac{10}{4}$.

A4 $2\frac{2}{4}$

Q5 This improper fraction is equivalent to 3.

A5 $\frac{9}{3}$

Q6 This mixed numeral comes directly after $\frac{9}{3}$.

A6 $3\frac{1}{3}$

Q7 This improper fraction is equivalent to 4.

A7 $\frac{12}{3}$

Q8 This improper fraction is equivalent to 6.

A8 $\frac{12}{2}$

Q9 This improper fraction is equivalent to $2\frac{2}{3}$.

A9 $\frac{8}{3}$

Q10 This mixed numeral is one third less than $\frac{8}{3}$.

A10 $2\frac{1}{3}$

Fractions – simplifying fractions

These fractions are all equivalent to one half: $\frac{1}{2}$ $\frac{2}{4}$ $\frac{6}{12}$ $\frac{75}{150}$ $\frac{3455}{6910}$

Which is the simplest? $\frac{1}{2}$

A fraction is in its simplest form when 1 is the only number that both numbers can be divided by. We simplify fractions to make reading and working with fractions easier.

1 Circle the simplest fraction in each group:

a $\frac{1}{2}$ $\frac{2}{4}$ $\frac{50}{100}$

b $\frac{33}{99}$ $\frac{3}{9}$ $\frac{1}{3}$

c $\frac{25}{100}$ $\frac{1}{4}$ $\frac{5}{20}$

d $\frac{2}{3}$ $\frac{6}{9}$ $\frac{16}{24}$

To find the simplest fraction, we divide both the numerator and the denominator by the same number. It makes sense for this to be the biggest number we can find so we don't have to keep dividing. This number is called the **Highest Common Factor (HCF)**.

Look at:

$$\frac{6}{18} = \frac{\boxed{?}}{\boxed{?}}$$

What is the biggest number that goes into both 6 and 18?

6 is the biggest number that goes into 18 and 6.

$$\frac{6 \div 6}{18 \div 6} = \frac{\boxed{1}}{\boxed{3}}$$

2 Find the highest common factor and then simplify:

a $\frac{15}{20}$ HCF is $\boxed{5}$ $\rightarrow \frac{15 \div 5}{20 \div 5} = \frac{\boxed{3}}{\boxed{4}}$

b $\frac{9}{30}$ HCF is $\boxed{3}$ $\rightarrow \frac{9 \div 3}{30 \div 3} = \frac{\boxed{3}}{\boxed{10}}$

c $\frac{16}{24}$ HCF is $\boxed{8}$ $\rightarrow \frac{16 \div 8}{24 \div 8} = \frac{\boxed{2}}{\boxed{3}}$

d $\frac{12}{36}$ HCF is $\boxed{12}$ $\rightarrow \frac{12 \div 12}{36 \div 12} = \frac{\boxed{1}}{\boxed{3}}$

3 Wally says he has simplified these fractions as far as he can. Is he right? If not, find the simplest fraction:

a $\frac{16}{20} \rightarrow \frac{8}{10} \rightarrow \frac{4}{5}$

b $\frac{50}{100} \rightarrow \frac{25}{50} \rightarrow \frac{5}{10} \rightarrow \frac{1}{2}$

c $\frac{24}{36} \rightarrow \frac{4}{6} \rightarrow \frac{2}{3}$

d $\frac{15}{20} \rightarrow \frac{3}{4}$

Fractions – simplifying fractions

4 Write the following fractions in their simplest form:

a $\frac{28}{49} = \frac{\boxed{4}}{\boxed{7}}$

b $\frac{12}{20} = \frac{\boxed{3}}{\boxed{5}}$

c $\frac{24}{42} = \frac{\boxed{4}}{\boxed{7}}$

d $\frac{13}{39} = \frac{\boxed{1}}{\boxed{3}}$

e $\frac{32}{36} = \frac{\boxed{8}}{\boxed{9}}$

f $\frac{9}{15} = \frac{\boxed{3}}{\boxed{5}}$

g $\frac{16}{48} = \frac{\boxed{1}}{\boxed{3}}$

h $\frac{15}{55} = \frac{\boxed{3}}{\boxed{11}}$

If you are not sure what the HCF is, guess, check and improve is a useful strategy. Try your choice out and then look at your new fraction.

Could it be any simpler? Is 1 the ONLY number that could go into both the numerator and the denominator?

5 Solve the following problems. Write your answers in the simplest form:

a Luke scored $\frac{16}{20}$ on a test. What fraction was incorrect?

$\frac{\boxed{1}}{\boxed{5}}$

b Marika scored $\frac{12}{20}$ on the same test. What fraction did she get right?

$\frac{\boxed{3}}{\boxed{5}}$

c 25 out of the 75 kids in Year 6 ride their bikes to school. What fraction does this represent?

$\frac{\boxed{1}}{\boxed{3}}$

d Out of the 26 students in 6F, 14 rate Maths as their favourite subject. What fraction is this?

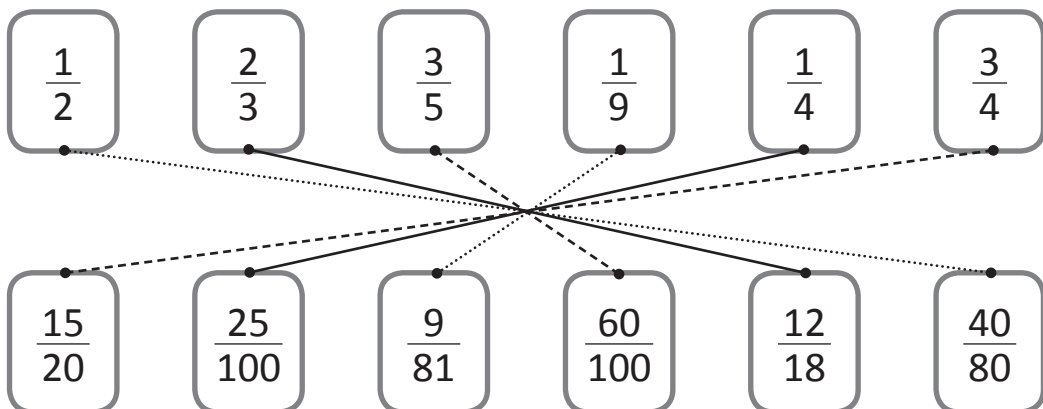
$\frac{\boxed{7}}{\boxed{13}}$

e What fraction did not choose Maths as their favourite subject?

$\frac{\boxed{6}}{\boxed{13}}$



6 Colour and match the fractions on the bottom row with their simplest form:



Fractions – comparing and ordering fractions

Comparing and ordering fractions with like denominators is a simple process:

When there are different denominators we need to rename the fractions so they have the same denominators. This lets us compare apples with apples.

Which is larger? $\frac{3}{4}$ or $\frac{5}{8}$

We know that $\frac{3}{4}$ is equivalent to $\frac{6}{8}$ so $\frac{3}{4}$ is larger than $\frac{5}{8}$

1 Order these fractions:

$1\frac{1}{2}$ $\frac{5}{4}$ $\frac{3}{4}$ $\frac{2}{4}$ $1\frac{3}{4}$ $\frac{1}{4}$ $\frac{4}{4}$

$\frac{1}{4}$ $\frac{2}{4}$ $\frac{3}{4}$ $\frac{4}{4}$ $\frac{5}{4}$ $1\frac{1}{2}$ $1\frac{3}{4}$



Hmm ... I had better make the mixed numbers into improper fractions as well. That will make them easier to compare.

THINK

2 Rename a fraction in each group so that you can compare them more easily. Circle the larger fraction:

a $\frac{1}{2}$ $\frac{2}{8}$

$\frac{4}{8}$

b $\frac{4}{8}$ $\frac{3}{4}$

$\frac{6}{8}$

c $\frac{2}{6}$ $\frac{1}{2}$

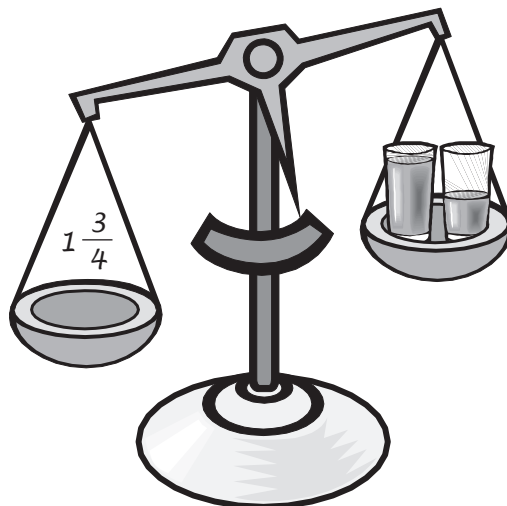
$\frac{3}{6}$

d $\frac{10}{12}$ $\frac{3}{4}$

$\frac{9}{12}$

3 Write or draw a fraction on the left that would result in the scale looking like this:

Answers will vary.



Remember with equivalent fractions, we think about what we did to get from one to the other:

$$\frac{2}{3} = \frac{8}{12}$$

× 4
× 4



REMEMBER

Fractions – comparing and ordering fractions

4 Find a partner to play this game with:

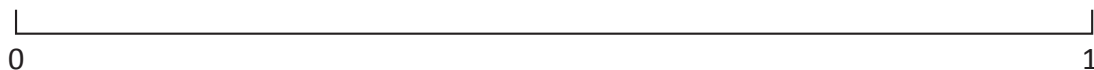
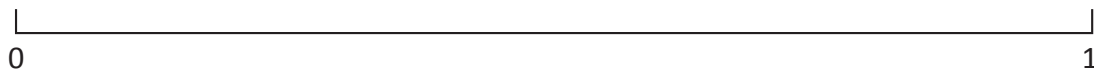
Name a fraction between 0 and 1 and place it on the number line. Your partner then has to name and place a fraction that fits between that fraction and 1. Then you have to find one that fits between their fraction and 1 and so on. The game continues until one player cannot think of a fraction, or can't fit one in.

You can challenge a fraction placement. If you are right, your partner has to remove their fraction. If you are wrong, they get to do the 'told you so' dance.

Answers will vary.



Alright, she put $\frac{2}{3}$
I am going to put $\frac{3}{4}$
because I know that
is more than $\frac{2}{3}$



5 These fractions are all out of order. Cut them out and put them in order from smallest to largest. Place any equivalent fractions on top of each other. There is a space for you to rename the fractions on each of the cards if this will help. Share your thinking with a partner.

Have they ordered them the same way?

$\frac{1}{2}$ $\frac{8}{16}$	$\frac{6}{8}$ $\frac{12}{16}$	$\frac{1}{4}$ $\frac{4}{16}$	$\frac{12}{16}$ $\frac{12}{16}$	$\frac{13}{16}$ $\frac{13}{16}$	$\frac{15}{16}$ $\frac{15}{16}$
$\frac{10}{8}$ $\frac{20}{16}$	$\frac{5}{8}$ $\frac{10}{16}$	$\frac{10}{16}$ $\frac{10}{16}$	$\frac{7}{8}$ $\frac{14}{16}$	$\frac{2}{8}$ $\frac{4}{16}$	$\frac{5}{16}$ $\frac{5}{16}$

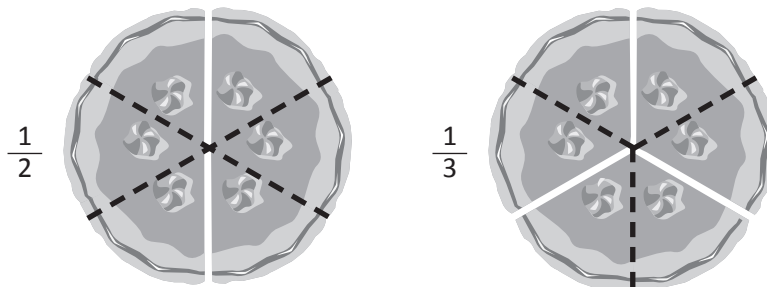
Fractions – renaming and ordering fractions

Sometimes we have to order and compare fractions with unrelated denominators such as $\frac{1}{4}$, $\frac{1}{6}$ and $\frac{1}{5}$.

To do this, we have to find one common denominator we can convert all the fractions to.

- 1 You have 2 cakes for a class party. One has been cut into halves and one into thirds. The problem is that you want each slice to be a fair fraction of the cakes.

- a Continue cutting the cakes so that each cake has the same number of fair slices:



- b If you had one of these new slices, what fraction of the cake would you receive?

1
6

That is an example of how we rename fractions. We find a way to re-divide the wholes so that they have the **same number of parts**. To do this efficiently we find the smallest shared multiple. This is then called the **Lowest Common Denominator (LCD)**:

$\frac{1}{2}$ The multiples of 2 are 2, 4, **6**, 8, ... $\frac{1}{3}$ The multiples of 3 are 3, **6**, 9, 12, 15, ...

6 is the LCD so we convert both fractions to sixths:

$$\frac{1}{2} \times \frac{3}{3} = \frac{3}{6}$$

$$\frac{1}{3} \times \frac{2}{2} = \frac{2}{6}$$

- 2 Rename these fractions by first finding the shared LCD and then converting the fractions. Use the multiplication table on the right to help you find the LCD:

a $\frac{1}{2}$ $\frac{1}{4}$ $\frac{1}{3}$

6	3	4
12	12	12

b $\frac{3}{6}$ $\frac{1}{2}$ $\frac{1}{3}$

3	3	2
6	6	6

c $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{6}$

4	3	2
12	12	12

× 2	× 3	× 4	× 5	× 6
2	3	4	5	6
4	6	8	10	12
6	9	12	15	18
8	12	16	20	24
10	15	20	25	30
12	18	24	30	36
14	21	28	35	42
16	24	32	40	48
18	27	36	45	54

Fractions – renaming and ordering fractions

- 3** Look at each group of fractions. Predict which you think is the largest and circle your prediction. Now, rename the fractions in the work space below so that each fraction in the group has the same denominator. Use a different colour to circle the largest fraction. Are there any surprises?

a $\frac{1}{2}$ $\left(\frac{2}{3}\right)$ $\frac{3}{9}$ b $\frac{2}{5}$ $\left(\frac{1}{2}\right)$ $\frac{1}{3}$ c $\left(\frac{3}{4}\right)$ $\frac{2}{3}$ $\frac{4}{8}$ d $\left(\frac{3}{4}\right)$ $\frac{3}{6}$ $\frac{3}{8}$

9	12	6
18	18	18

12	15	10
30	30	30

18	16	12
24	24	24

18	12	9
24	24	24

- 4** This time, rename the fractions and circle the largest. Underline the smallest.

a $\frac{3}{8}$ $\frac{2}{4}$ $\left(\frac{5}{6}\right)$ b $\frac{4}{7}$ $\frac{1}{2}$ $\left(\frac{11}{14}\right)$ c $\frac{1}{3}$ $\frac{5}{8}$ $\left(\frac{4}{6}\right)$ d $\left(\frac{3}{4}\right)$ $\frac{2}{3}$ $\frac{1}{2}$

9	12	20
24	24	24

8	7	11
14	14	14

8	15	16
24	24	24

9	8	6
12	12	12

- 5** For each fraction write a larger fraction below. The new fraction must have a different denominator. It can have a different numerator.

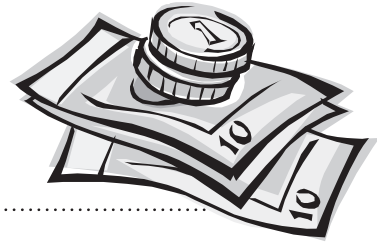
$\frac{1}{2}$	$\frac{1}{3}$	$\frac{2}{3}$	$\frac{4}{5}$	$\frac{9}{15}$
<div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>	<div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>	<div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>	<div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>	<div style="border: 1px solid black; width: 40px; height: 40px; margin: 0 auto;"></div>

Answers will vary.



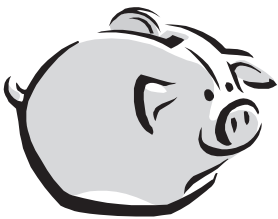
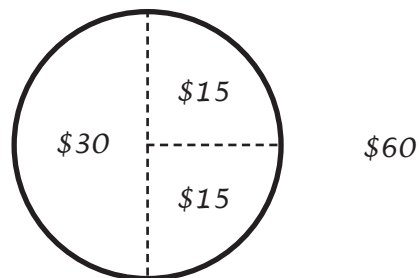


In this activity you will solve money problems. Working backwards is a useful maths working strategy to use here.

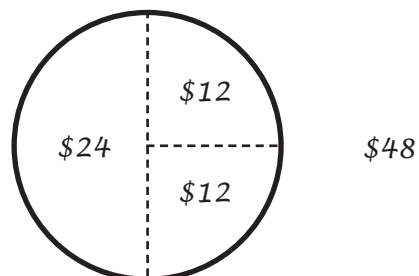


Use the fraction pies to help you solve the following problems:

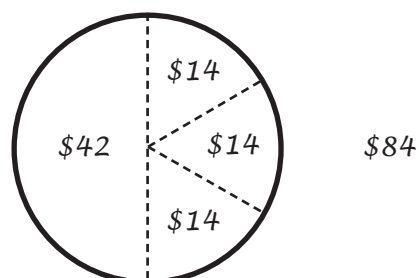
Sarah's gran gave her some money for her birthday. Sarah saved $\frac{1}{2}$ of the money and spent $\frac{1}{4}$ of the money on a book. That left her with \$15 in her purse. How much money did her Gran give her?



Martha opened her piggy bank and decided to spend it this way: $\frac{1}{2}$ on magazines; $\frac{1}{4}$ on snacks; $\frac{1}{4}$ on a necklace. The necklace cost \$12. How much money did she have in her piggy bank?



Ali went to the show. He spent $\frac{1}{2}$ of his money on rides and $\frac{1}{3}$ of what was left on a dagwood dog, some chips and some fairy floss. That left him with \$28 to spend on show bags. How much money did he have to begin with?





Getting ready

Sam and his mates decide to go trick or treating one Halloween. They then divvy up the loot.



What to do

Use the chart on the right to work out the answers to the problems below:

Total
50 mini chocolate bars
18 gob stoppers
16 Chuppa Chups
12 Wizz Fizzes
4 all day suckers
2 Easter eggs
1 turnip



- a In the opening round, Sam gets $\frac{2}{5}$ of the mini chocolate bars and $\frac{1}{4}$ of the Chuppa Chups. How many of each does he get?
20 mini chocolate bars and 4 Chuppa Chups.
- b George wanted all the gob stoppers. In a tense negotiation with Sam, he managed to score $\frac{2}{3}$ of them. How many did he get? How many did he miss out on?
12 gob stoppers. He missed out on 6.
- c To get his share of the gobstoppers, Sam has to trade off $\frac{1}{2}$ of the Chuppa Chups he received in Question a. How many does he lose?
2 Chuppa Chups.
- d Mara gets all the Wizz Fizzes, $\frac{1}{2}$ the all day suckers, and the remaining $\frac{3}{5}$ of the chocolate bars. In total, how many items does she get?
- | | |
|---------------------|----------|
| 12 Wizz Fizzes | |
| 2 suckers | 44 items |
| + 30 chocolate bars | |
| 44 | |
- e Here is a fraction sentence that shows how the gob stoppers were shared:
 $\frac{1}{3} + \frac{2}{3} = \frac{3}{3}$ or 1 whole. Write the fraction sentence that shows how the chocolate bars were shared.
- $$\frac{2}{5} + \frac{3}{5} = \frac{5}{5} = 1 \text{ whole}$$
- f Mara decides to give $\frac{1}{4}$ of her Wizz Fizzes to George. Write the fraction sentence to show how many she has left. Now, write the sentence using whole numbers.
- $$1 - \frac{1}{4} = \frac{3}{4}$$
- $$12 - 3 = 9$$

Decimal fractions – tenths, hundredths and thousandths

Common fractions and decimal fractions are related as they both show parts of a whole. In common fractions, we divide a whole into parts such as halves or sixths.

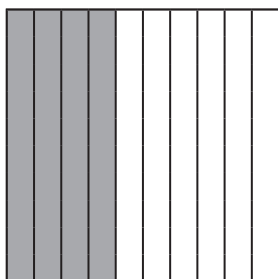
In decimal fractions, the whole is partitioned using the base 10 system – into tenths, then hundredths, then thousandths and so on.

We use a decimal point after the unit to indicate the end of whole numbers: 6.42

If the number has no whole numbers, we use a zero to make sure we don't miss the decimal point: 0.42

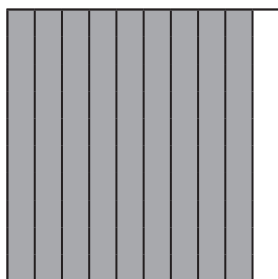
1 Divide these wholes into tenths and shade the specified amounts. Write each as a decimal fraction:

a



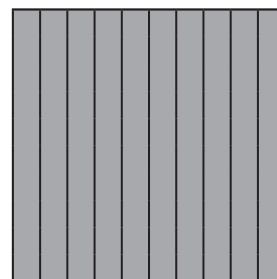
$$\frac{4}{10} \quad \boxed{0 \cdot 4}$$

b



$$\frac{9}{10} \quad \boxed{0 \cdot 9}$$

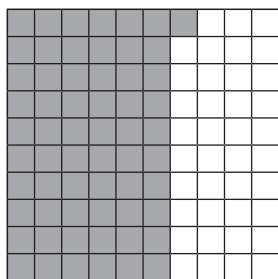
c



$$\frac{10}{10} \quad \boxed{1 \cdot 0}$$

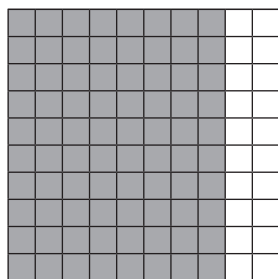
2 Now divide these wholes into hundredths and shade the specified amounts. Write each as a decimal fraction:

a



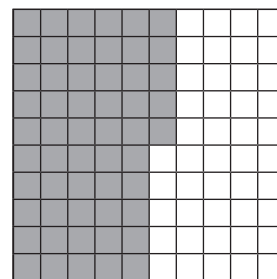
$$\frac{61}{100} \quad \boxed{0 \cdot 6 \quad 1}$$

b



$$\frac{80}{100} \quad \boxed{0 \cdot 8 \quad 0}$$

c



$$\frac{55}{100} \quad \boxed{0 \cdot 5 \quad 5}$$

3 Express these as decimal fractions:

a 6 tenths, 7 hundredths, 4 thousandths

$$\boxed{0 \cdot 6 \quad 7 \quad 4}$$

b $\frac{432}{1000}$ $\boxed{0 \cdot 4 \quad 3 \quad 2}$

c 4 tenths, 9 hundredths, 3 thousandths

$$\boxed{0 \cdot 4 \quad 9 \quad 3}$$

d $\frac{589}{1000}$ $\boxed{0 \cdot 5 \quad 8 \quad 9}$

e 0 tenths, 2 hundredths, 9 thousandths

$$\boxed{0 \cdot 0 \quad 2 \quad 9}$$

f $\frac{7}{1000}$ $\boxed{0 \cdot 0 \quad 0 \quad 7}$

g 4 thousandths

$$\boxed{0 \cdot 0 \quad 0 \quad 4}$$

h $\frac{1000}{1000}$ $\boxed{1 \cdot 0 \quad 0 \quad 0}$

Decimal fractions – reading and writing decimals

When we write decimals we follow this place order:

Thousands	Hundreds	Tens	Units	Tenths	Hundredths	Thousandths
			2	2	5	6

Numbers **before** the decimal point are whole numbers.

Numbers **after** the decimal point are parts of a whole number.

The further the digit is to the left in the number, the greater its value. The further it is to the right, the smaller its value.

- 1 What is the value of the digit in bold? Tick the correct column:

	Thousands	Hundreds	Tens	Units	Tenths	Hundredths	Thousandths
a 5. 8 92					•	✓	
b 13. 0 5					•	✓	
c 7 63.22		✓			•		
d 89. 0 21				✓	•		
e 100. 0 01					•		✓
f 560. 4 5					•	✓	
g 31 2 .956			✓		•		

- 2 Read each number and write it as a decimal:

- a four units, one hundred and twenty two thousandths 4.122
- b one hundred and eleven, and sixty five hundredths 111.65
- c three hundred, and forty two thousandths 300.042
- d four thousand, and twelve hundredths 4000.12
- e twelve, and 13 thousandths 12.013
- f two hundred and thirteen, and forty-three hundredths 213.43

Watch out for the commas!
They indicate the end of whole numbers.



CHECK

- 3 These answers are all close but incorrect. Write the correct answers:

- | | | |
|---|------------------------------|--------------|
| a twenty seven tenths is written as 0.27 | No it's not, it's written as | <u>2.7</u> |
| b forty eight hundredths is written as 0.048 | No it's not, it's written as | <u>0.48</u> |
| c 9000 thousandths is written as 0.009 | No it's not, it's written as | <u>9.0</u> |
| d eleven and 12 hundredths is written as 11.012 | No it's not, it's written as | <u>11.12</u> |
| e 167 hundredths is written as 16.7 | No it's not, it's written as | <u>1.67</u> |

Decimal fractions – comparing and ordering decimals

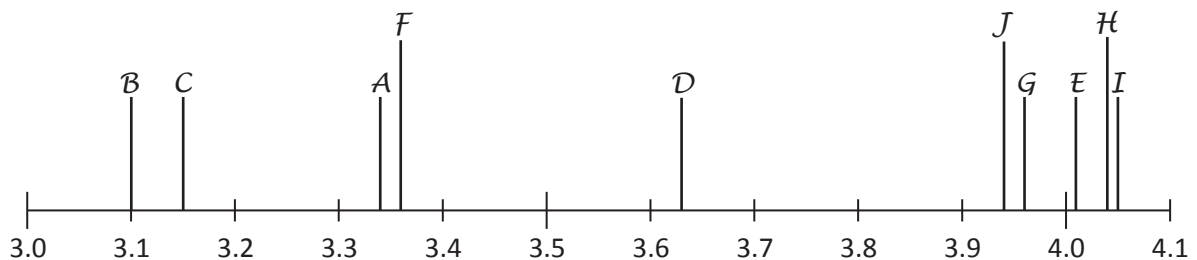
We need to carefully consider the place value of digits when ordering and comparing decimals.



	Name	Distance
A	Spitter Macgee	3.34 m
B	Did You See That One Big-noter	3.1 m
C	Secret-ingredient Spitski	3.15 m
D	Dead-eye Jones	3.63 m
E	The Long Distance Shooter	4.01 m
F	Sally Straw	3.36 m
G	Technique Tezza	3.96 m
H	Lone Shooter	4.04 m
I	Double Or Nothing Danielle	4.05 m
J	Shoot Dog	3.94 m

- 1 6A has a very cool teacher who decides to harness, not ban, the class' current obsession with pea shooting. After a week of intense training, a shoot-off occurs. The results for the top ten shooters are tabled on the right.

Place the students on the number line. The first one has been done for you.



- 2 Use the above information to answer the following questions:

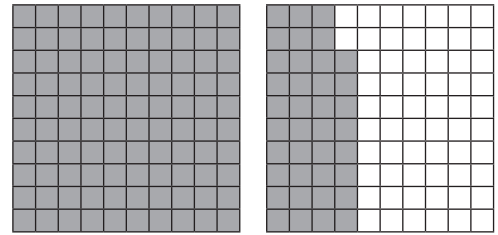
- Who shot the furthest on the day? Double Or Nothing Danielle
- Whose shot was the shortest? Did You See That One Big-noter
- Which students' shots were 1 hundredth of a metre apart?
Lone Shooter and Double Or Nothing Danielle
- What was the difference between the shots of Shoot Dog and Spitter Macgee? 0.6 m
- Do you think you could beat this? Something to try at home perhaps? Even 6A's teacher eventually had enough of the pea shooting.

Answers will vary.

Decimal fractions – renaming decimals

We can express the same decimal fraction in different ways.
This shows 138 hundredths.

We can also express this as 1 unit, 3 tenths and 8 hundredths
or 13 tenths and 8 hundredths **or** 1 unit and 38 hundredths.



1 Rename these fractions:

- a 37 hundredths is also tenths + hundredths
- b 53 hundredths is also tenths + hundredths
- c 99 hundredths is also tenths + hundredths
- d 6 tenths and 3 hundredths is also hundredths
- e 4 tenths and 9 hundredths is also hundredths
- f 4 tenths, 9 hundredths and 8 thousandths is also thousandths
- g 0 tenths, 5 hundredths and 8 thousandths is also thousandths

It may help to write these numbers in their decimal forms.

2 Now try these. Fill in the missing information:

- a 4 units = 40 tenths = 400 hundredths = 4 000 thousandths
- b 7 units = 70 tenths = 700 hundredths = 7 000 thousandths
- c 2.5 units = 25 tenths = 250 hundredths = 2 500 thousandths
- d 9 units = 90 tenths = 900 hundredths = 9 000 thousandths



THINK

3 Rename these numbers as many ways as you can. Use the abbreviation: H for hundredths, T for tenths and U for units:

5.67	2.52	9.81
<u>5 U 67 H</u>	<u>2 U 52 H</u>	<u>9 U 81 H</u>
<u>5 U 6 T 7 H</u>	<u>2 U 5 T 2 H</u>	<u>9 U 8 T 1 H</u>
<u>56 T 7 H</u>	<u>25 T 2 H</u>	<u>98 T 1 H</u>
<u>567 H</u>	<u>252 H</u>	<u>981 H</u>

Decimal fractions – rounding

We often round decimals to a particular place value. We do this to make the numbers easier to work with.

Look at 2.685. We can round this to the nearest whole number, tenth or hundredth.

Let's round it to the nearest tenth. To do this, we look at the number in the hundredths place.

This is 8, which is closer to 10 than 1, so we round the tenth up. The rounded number is now 2.7

1 Round these numbers to the nearest tenth:

a 67.23 67.2

b 48.07 48.1

c 124.78 124.8

d 90.14 90.1

e 54.53 54.5

f 7.06 7.1

If the rounding number is a 1 to 4, it rounds down. If it is 5 to 9, it rounds up.

2 Now round these numbers to the nearest hundredth:

a 58.127 58.13

b 70.345 70.35

c 45.007 45.01

d 78.134 78.13

e 89.036 89.04

f 36.231 36.23



REMEMBER

3 Use a calculator to perform the following operations. Round the answers to the nearest tenth:

a $132.4 \div 5 =$ 26.5

b $178 \div 8 =$ 22.3

c $125.3 \div 4 =$ 31.3

d $223 \div 4 =$ 55.8

e $12 \div 7 =$ 1.7

f $123.52 \div 4 =$ 30.9

4 Look at the following meal options.

a Round each price to the nearest dollar and total the estimated cost of each option below:

Choice 1		
Hamburger	\$4.95	\$5
Can of drink	\$2.25	\$2
Large chips	\$1.15	\$1
Total		\$8

Choice 2		
Noodles with prawns	\$7.95	\$8
Green tea	\$0.95	\$1
3 Crab cakes	\$2.98	\$3
Total		\$12

Choice 3		
Salad roll	\$5.15	\$5
Juice	\$2.25	\$2
Cookie	\$1.95	\$2
Total		\$9

b You have \$10. Circle the choices you can afford.

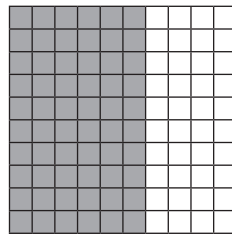
Decimal fractions – percentages

Percent comes from the Latin 'per centum' and means parts per hundred. It is expressed using the symbol %.

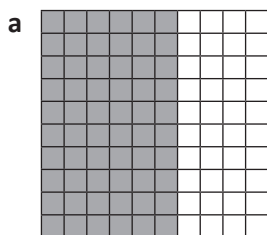
Here, 60% has been shaded. This is the same as 60 hundredths.

$$\frac{60}{100} = 0.60 = 60\%$$

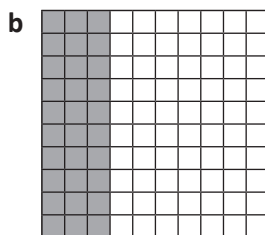
We commonly use percentages in sales – *25% off everything TODAY ONLY*; on tests – *I got 85%*; and when we are gathering and reporting on data – *78% of people surveyed love chocolate*.



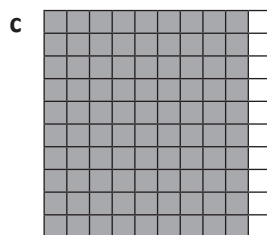
1 Fill in the missing values:



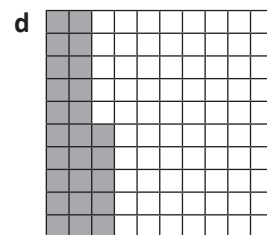
$\frac{60}{100}$	0.6	60%
------------------	-----	-----



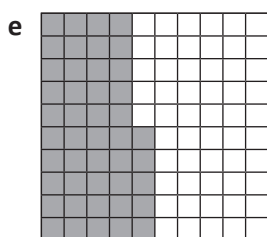
$\frac{30}{100}$	0.3	30%
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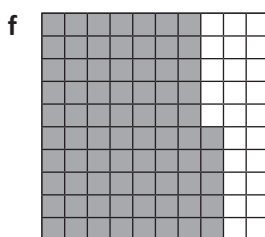
$\frac{90}{100}$	0.9	90%
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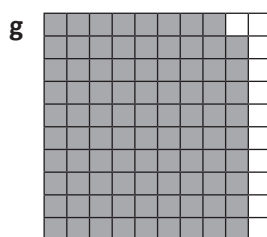
$\frac{25}{100}$	0.25	25%
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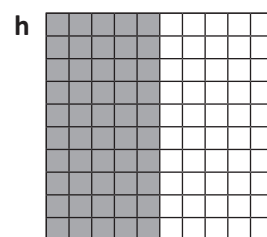
$\frac{45}{100}$	0.45	45%
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$\frac{75}{100}$	0.75	75%
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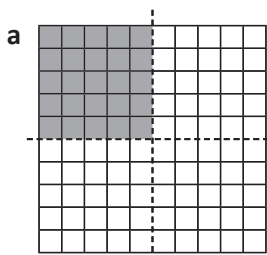
$\frac{89}{100}$	0.89	89%
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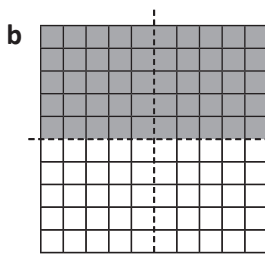
$\frac{50}{100}$	0.5	50%
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It is useful to know some common percentages such as 25%, 50%, 75% or 100%.

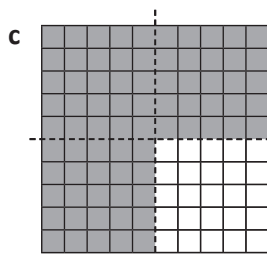
2 Shade the grids to show the following percentages:



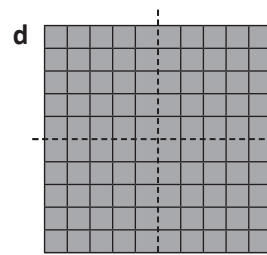
$\frac{1}{4}$	0.25	25%
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$\frac{1}{2}$	0.5	50%
---------------	-----	-----



$\frac{3}{4}$	0.75	75%
---------------	------	-----

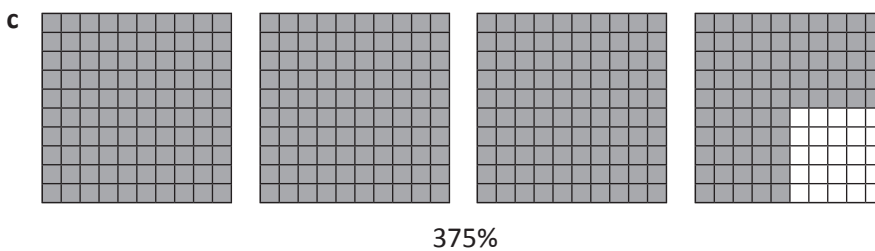
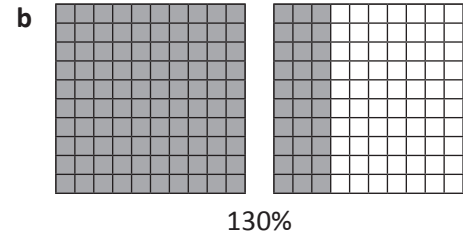
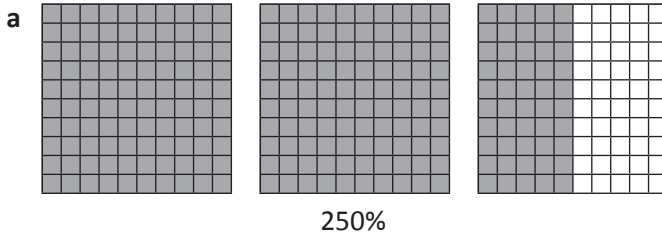


$\frac{4}{4}$	1.0	100%
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Decimal fractions – percentages

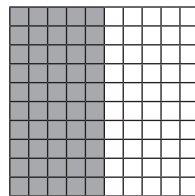
Not all percentage values are whole numbers between 1 and 100. We can have such things as 300% growth or percentages that contain decimals such as 3.5%.

3 Shade the grids to show the following percentages:

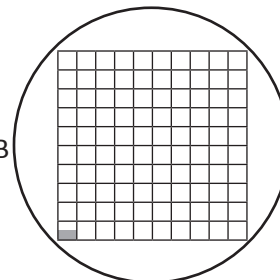


4 How would you show half a percent? Circle the option you think is correct. Discuss your choice with a partner. Do they agree?

Option A

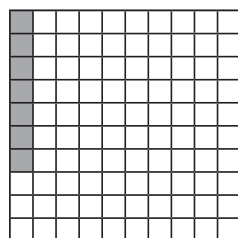


Option B

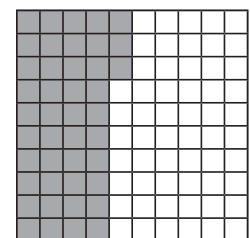


5 100 people were surveyed. They were asked to nominate their preferred way of eating vegetables. Shade the grids to show the survey results:

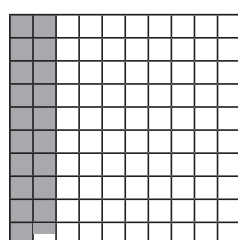
a 7% preferred their veggies boiled till they were all soggy and watery.



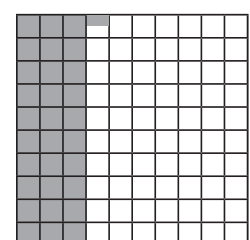
b 43% preferred their veggies stir fried.



c 19.5% preferred their veggies raw.



d 30.5% did not care how they were prepared because they weren't going to eat them anyway.





Getting ready

In this activity you are going to design a survey and then ask 100 people your questions. You will then find a way to communicate your results.

Work in a small group.



What to do

As a group, think about what information you are going to gather. Some things to consider might be:

- What kind of answers are you after?
- Will you provide options? How many? What if someone gives an answer you haven't included in your list? What if you get 100 different answers?
- Who is your target audience and when will you ask them? If you are surveying kids about their favourite ice cream flavours, asking at lunch times would be a good time. If you want adult responses, when is the best time to be able to talk to 100 adults?
- How will you record the answers?

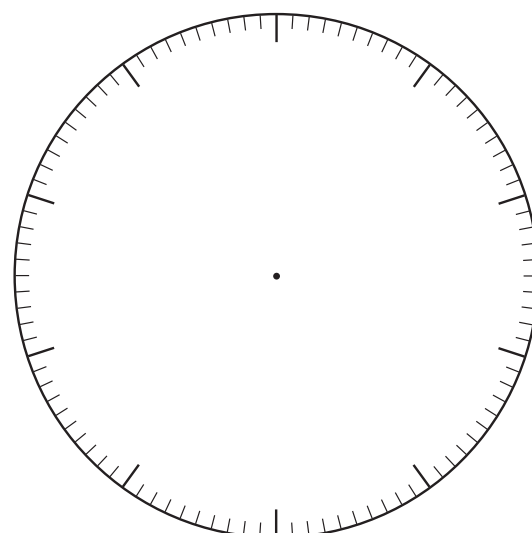
Plan your survey and run it by your teacher. If it all looks good, conduct it.



What to do next

Use a pie graph to represent your information. You may use this model below or create your own using a spreadsheet program.

Answers will vary





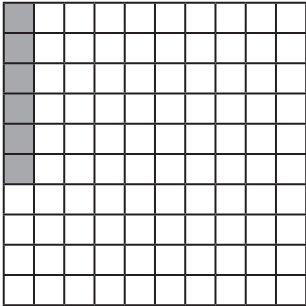
Getting ready

We have been using 100 grids to represent percentage, with each square representing 1%.



What to do

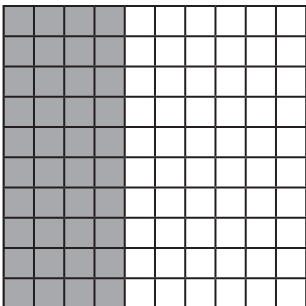
These grids are set up a little differently. Work with a partner to figure out what each square represents and then answer the questions.



Problem 1

These 6 squares have a value of 36.

- What is the value of 1 square? 6
- What is the value of the entire grid? 600
- If 50% of the grid is shaded, what value is shaded? 300

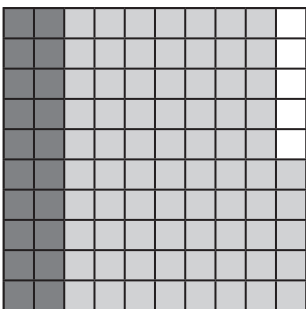


Problem 2

There are 140 convenience stores in Smallville.

- 40% of these stock your favourite Slurpee flavour. Use the grid to represent this information.
- How many stores sell your favourite flavour? 56

300 people



Problem 3

- If this grid represents 300 people, what does each square represent? 3 people
- How many people are represented by ten squares? 30
- 60 of the 300 people like watching sports. Represent this on the grid in red.
- 225 people prefer playing sport to watching it. Represent this in green.

Fractions of an amount – finding fractions

What process do we use to find fractions of amounts?

When we find $\frac{1}{4}$ of 20, we are sharing 20 into 4 groups. We use **division** to find fractions.

- 1 Warm up with this puzzle. Use division to find the answer to each clue. The solved puzzle will tell you the name of a very important day of the year.

<u>W</u>	<u>O</u>	<u>R</u>	<u>L</u>	<u>D</u>	<u>M</u>	<u>A</u>	<u>T</u>	<u>H</u>	<u>S</u>
2	11	25	4	9	3	8	5	75	10

<u>D</u>	<u>A</u>	<u>Y</u>
9	8	50

$$L = \frac{1}{4} \text{ of } 16$$

$$Y = \frac{1}{2} \text{ of } 100$$

$$A = \frac{1}{12} \text{ of } 96$$

$$D = \frac{1}{7} \text{ of } 63$$

$$O = \frac{1}{2} \text{ of } 22$$

$$S = \frac{1}{100} \text{ of } 1000$$

$$H = \frac{1}{4} \text{ of } 300$$

$$T = \frac{1}{11} \text{ of } 55$$

$$M = \frac{1}{3} \text{ of } 9$$

$$W = \frac{1}{2} \text{ of } 4$$

$$R = \frac{1}{4} \text{ of } 100$$

Put this date in your diary! Tell your friends!



- 2 We use fractions of time regularly in our lives. Use the clock to work out:

a What fraction of an hour is 15 minutes?

1
4

b What fraction of an hour is 30 minutes?

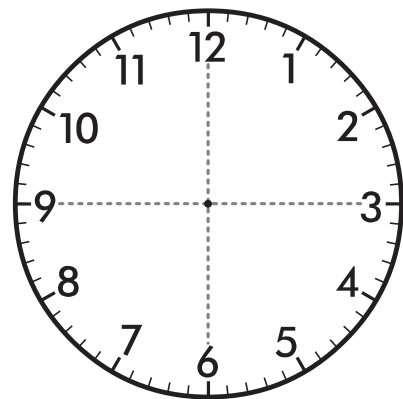
1
2

c What fraction of an hour is 45 minutes?

3
4

d What fraction of an hour is 20 minutes?

1
3



e If Lucas practises guitar from 4:20 to 4:35 each day, what fraction of an hour does this represent?

1
4

f Patrick practises soccer for 1 hr 15 min. How would you express that as an improper fraction?

5
4

g Find 3 time spans that represent $\frac{1}{3}$ of an hour.

Answers will vary and may include:

3.00 to 3.20 4.30 to 4.50 11.20 to 11.40

Fractions of an amount – finding fractions

Once we know how to find one part of a group, we can use this to find other fractional amounts:

To find $\frac{2}{3}$ of 9, we first find $\frac{1}{3}$ of 9 $\longrightarrow 9 \div 3 = 3$ $\frac{1}{3}$ of 9 = 3

$\frac{2}{3}$ of 9 is 2 times this $\longrightarrow 2 \times 3 = 6$ $\frac{2}{3}$ of 9 = 6

3 Find the following fractional amounts:

a $\frac{2}{4}$ of 12 =

b $\frac{5}{6}$ of 30 =

c $\frac{3}{4}$ of 24 =

d $\frac{3}{8}$ of 96 =

e $\frac{9}{10}$ of 20 =

f $\frac{3}{5}$ of 350 =

4 The Walsh kids fight like cats and dogs over computer time and their dad has had enough. He has drawn up a schedule and says that if they don't stick to it, he will hide the keyboard till Christmas and cut off the internet. Help the kids work out their daily allocation and save them from a fate worse than death:

a How many minutes does each kid get each day?

Dylan

Nina

Natasha

b How many minutes must Dylan spend on study?

45 minutes

c How many minutes will Nina spend on Mathematics?

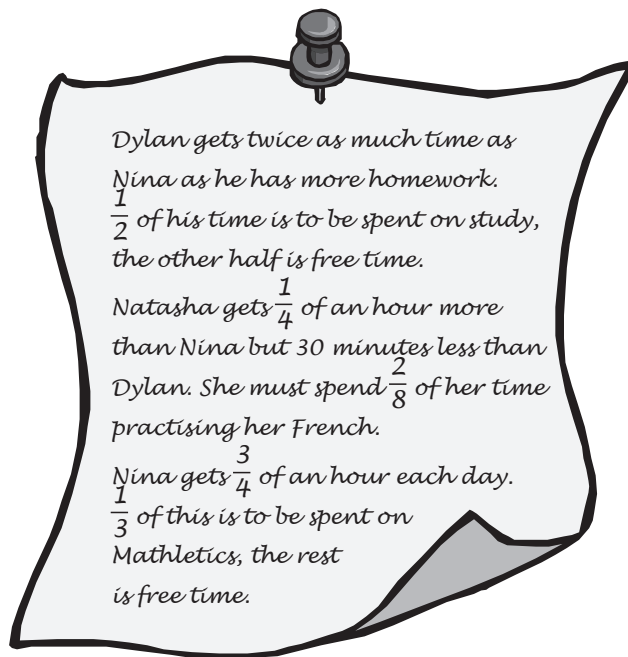
15 minutes

d Express the time allocations as fractions of an hour:

Dylan $\frac{3}{2}$ or $1\frac{1}{2}$

Nina $\frac{3}{4}$

Natasha $\frac{1}{1}$



This one is a puzzle. Read all the clues carefully – one of them is your starting point. Once you have solved that all important first clue, the rest will follow.

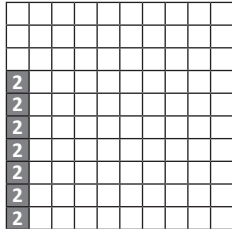


Fractions of an amount – percentage

We often have to find percentages in real life such as '40% off – today only!'

40% of 100 is $\frac{40}{100}$ or 40. A \$100 item would be reduced by \$40.

That's easy if everything costs \$100 but how do we find percentages of numbers other than 100? There are a number of ways to do this – here are some of them.



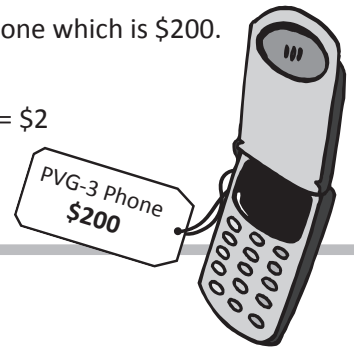
Look at this 100 grid. It represents the total cost of this phone which is \$200.

Each of the 100 squares represents 1% of this.

To find the value of a single square we divide: $\$200 \div 100 = \2

Each square or percent represents \$2.

How do we then find 7% of \$200? $7 \times \$2 = \14 .



1 Use the 100 grid to calculate:

a 5% of \$200 is \$10

b 20% of \$200 is \$40

c 10% of \$200 is \$20

d 22% of \$200 is \$44

e 15% of \$200 is \$30

f 50% of \$200 is \$100

g If the store advertises a sale of 15% off the cost of the phone, what is the saving in dollars? \$30

2 Use the 100 grid to calculate the following. 1 square represents 3 people:

300 people

a 8% of 300 people is 24

b 50% of 300 people is 150

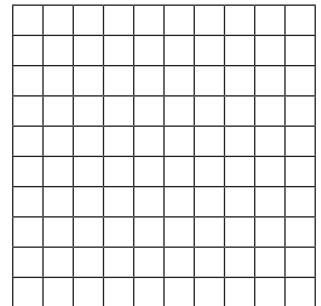
c 25% of 300 people is 75

d 40% of 300 people is 120

e 12% of 300 people is 36

f 80% of 300 people is 240

g If 65% of the 300 people surveyed liked chocolate, how many people liked chocolate? 195



3 Patterns can also help us understand percentages. Use patterns to calculate. The first row has been done for you.

10% of 40 is 4

5% of 40 is 2

20% of 40 is 8

10% of 50 is 5

5% of 50 is 2.5

20% of 50 is 10

10% of 60 is 6

5% of 60 is 3

20% of 60 is 12

10% of 100 is 10

5% of 100 is 5

20% of 100 is 20

10% of 500 is 50

5% of 500 is 25

20% of 500 is 100

10% of 1000 is 100

5% of 1000 is 50

20% of 1000 is 200

10% of 3000 is 300

5% of 3000 is 150

20% of 3000 is 600

Fractions of an amount – percentage

We can use fractions to help us calculate percentages.

How can we calculate 25% of 80?

We know that 25% is the same as $\frac{1}{4}$. To find $\frac{1}{4}$ of 80 we divide by 4.

$$80 \div 4 = 20$$

$$25\% \text{ of } 80 \text{ is } 20.$$

$$\frac{1}{2} = 50\%$$

$$\frac{1}{4} = 25\%$$

$$\frac{1}{3} = 33\frac{1}{3}\%$$

$$\frac{1}{5} = 20\%$$

$$\frac{1}{10} = 10\%$$

$$\frac{3}{4} = 75\%$$

4 Use your knowledge of fractions to calculate the percentages:

- | | | |
|--|--|---|
| a 25% of 120 is 30 | b 50% of 250 is 125 | c 20% of 50 is 10 |
| $\frac{1}{4}$ of 120 = 30 | $\frac{1}{2}$ of 250 = 125 | $\frac{1}{5}$ of 50 = 10 |
| $120 \div 4 = \underline{\quad 30 \quad}$ | $250 \div 2 = \underline{\quad 125 \quad}$ | $50 \div 5 = \underline{\quad 10 \quad}$ |
| <hr/> | | |
| d 25% of 16 is 4 | e $33\frac{1}{3}\%$ of 66 is 22 | f 75% of 80 is 60 |



Calculators are also handy for working out percentages. This is how we calculate 40% of 50:

We enter 5 0 x 4 0 % Our answer appears 2 0

5 Use a calculator to find these percentages:

- | | | |
|--|--|---|
| a 20% of 300 mL = 60 mL | b 35% of 280 mL = 98 mL | c 15% of 800 kg = 120 kg |
| d 6% of 70 km = 4.2 km | e 25% of 150 mL = 37.5 mL | f 9% of \$700 = \$63 |
| g 15% of 400 = 60 | h 18% of 300 mL = 54 mL | i 90% of 1000 = 900 |

6 The answer is 75. Use a calculator to work out the percentages and tick all the squares that match the answer:

<input checked="" type="checkbox"/> What is 25% of 300?	<input checked="" type="checkbox"/> What is 75% of 100?	<input checked="" type="checkbox"/> What is 10% of 750?	<input type="checkbox"/> What is 15% of 55?
<input type="checkbox"/> What is 45% of 180?	<input type="checkbox"/> What is 35% of 300?	<input checked="" type="checkbox"/> What is 50% of 150?	<input checked="" type="checkbox"/> What is 20% of 375?



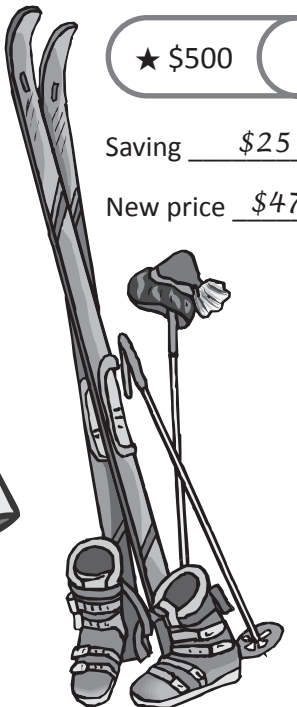


Fractions of an amount – finding discounts

We have to calculate discounts quite often in real life. Stores have many special offers and canny consumers can quickly calculate the savings to help them make decisions about their purchases.

- 1 How much would you save if the following discounts were offered? Choose a method to calculate:

 Plasma TV \$1000	 DVD \$12 each	 Ticket \$50 each	 Puppy \$250
10% off \$100	10% off \$1.20	10% off \$5	10% off \$25
25% off \$250	25% off \$3	25% off \$12.50	25% off \$62.50
50% off \$500	50% off \$6	50% off \$25	50% off \$125
60% off \$600	60% off \$7.20	60% off \$30	60% off \$150

- 2 You are helping your grandpa with his holiday shopping at Savers. Everything in the store marked ★ is 5% off, everything marked ★★ is 15% off and everything marked ★★★ is 20% off. Help your grandpa calculate both the savings and the new costs:

 ★★ \$20 Saving \$3 New price \$17	 ★ \$85 Saving \$4.25 New price \$80.75	 ★ \$500 Saving \$25 New price \$475
 ★★★ \$15 Saving \$3 New price \$12	 ★★ \$40 Saving \$6 New price \$34	



Get ready to shop! Work in a small group for this activity. You'll all need a copy of this page. Calculators may not be used.



You are each going to fill your own mall with things you like, then another group member will decide what kind of discounts you can have on each item.

Then you'll each race around your own mall calculating the new prices.

You may keep any items you calculate correct prices for. You have to put back any mistakes!



In each shop is a price tag. Next to each tag, draw something you think you'd like that would probably cost around this amount.

Now switch your paper with someone else in the group. Choose a discount of 5%, 10%, 20%, 25% or 50% to put next to the price. You must apply each discount at least once.

When everyone in your group is done, switch your pages back. On 'go', start calculating. Who finishes first? The game continues until everyone finishes their calculations.

Use a calculator to check everyone's maths. Who kept all their purchases? Excellent shopping.

	•\$10 ____% \$____	•\$100 ____% \$____	
•\$160 ____% \$____			•\$40 ____% \$____
•\$320 ____% \$____	•\$20 ____% \$____	•\$20 ____% \$____	•\$120 ____% \$____

**Getting ready**

Solve these shopping dilemmas. You can work with a partner or by yourself.
Show your mathematical reasoning for each problem.

**What to do**

DILEMMA 1 You have been eyeing off a new pair of jeans available at your local jeans shop and also online. They are \$100 at both suppliers.

In the sales, your jeans shop offers a discount of 20%, followed by a further reduction of 40% on the marked sale price. The online supplier offers a straight 60% discount.

Are these discounts the same? If not, which is the better deal?

No. Online store \$40 and Shop \$48

The online store is the better deal.



DILEMMA 2 Would you rather become 50% poorer and then 50% richer *or* become 50% richer and then 50% poorer?

They result in the same answer.

DILEMMA 3 The new game you want costs \$175 at one store and \$180 at another. The first store then offers a discount of 5% while the second offers a discount of 10%.

Which deal gives you the cheapest price?

Second store \$162

Calculating – adding and subtracting common fractions

How do we add or subtract fractions? Look at this example:

We had a movie marathon on the weekend. On Saturday, we watched movies for $7\frac{1}{4}$ hours and on Sunday we watched for $5\frac{1}{4}$ hours. How many hours did we spend watching movies in total?

$$7\frac{1}{4} + 5\frac{1}{4} =$$

First we add the whole numbers: $7 + 5 = 12$. Then we add the fractions: $\frac{1}{4} + \frac{1}{4} = \frac{1}{2}$

Then we add the two answers together: $12 + \frac{1}{2} = 12\frac{1}{2}$

We use the same process to subtract fractions.

1 Solve these problems:

a $\frac{1}{3} + 2\frac{1}{3} = \boxed{2}\frac{\boxed{2}}{\boxed{3}}$

b $2\frac{3}{4} - 1\frac{2}{4} = \boxed{1}\frac{\boxed{1}}{\boxed{4}}$

c $1\frac{2}{5} + 3\frac{1}{5} = \boxed{4}\frac{\boxed{3}}{\boxed{5}}$

d $\frac{1}{5} + 6\frac{2}{5} = \boxed{6}\frac{\boxed{3}}{\boxed{5}}$

e $1\frac{3}{12} - \frac{1}{12} = \boxed{1}\frac{\boxed{2}}{\boxed{12}}$

f $7\frac{4}{12} - 3\frac{2}{12} = \boxed{4}\frac{\boxed{2}}{\boxed{12}}$

2 Express these as fraction sentences. Solve them:

- a Sarah and Rachel go to a trash and treasure sale. Sarah buys $3\frac{1}{4}$ boxes of trash and Rachel buys $2\frac{1}{4}$ boxes of treasure. How much do they buy in total?

$$3\frac{1}{4} + 2\frac{1}{4} = 5\frac{2}{4} = 5\frac{1}{2} \text{ boxes}$$

- b You have $2\frac{3}{4}$ boxes of chocolates and you eat $1\frac{1}{4}$ boxes. How many boxes do you have left?

$$2\frac{3}{4} - 1\frac{1}{4} = 1\frac{2}{4} = 1\frac{1}{2} \text{ boxes}$$

- c Before World Maths Day, Akhil practices Live Mathletics for $4\frac{1}{3}$ hours on Monday and $2\frac{1}{3}$ hours on Tuesday. How many hours of practice has he put in altogether?

$$4\frac{1}{3} + 2\frac{1}{3} = 6\frac{2}{3} \text{ hours}$$

- d Aman really gets into a sport for a while then drops it and moves on to his latest craze. As a consequence, he has five and a half cupboards of old sports equipment. His mother makes him take some of it to the local charity shop. This leaves him with 2 full cupboards. How much has he taken to the shop?

$$5\frac{1}{2} - 2 = 3\frac{1}{2}$$

3 What numbers could go in the boxes? *Answers will vary.*

a $\boxed{}\frac{\boxed{}}{\boxed{}} + 1\frac{\boxed{}}{\boxed{}} = 5\frac{3}{4}$

b $\boxed{}\frac{\boxed{}}{\boxed{}} - \boxed{}\frac{\boxed{}}{\boxed{}} = 3\frac{1}{6}$

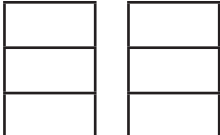
Calculating – adding and subtracting common fractions

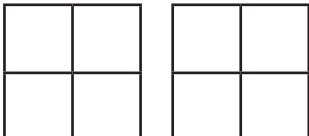
Look at this problem: $7\frac{2}{4} + 3 + \frac{3}{4}$

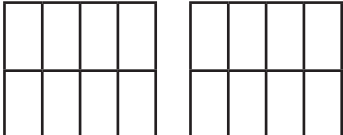
Our answer is $10\frac{5}{4}$ which is a little confusing.

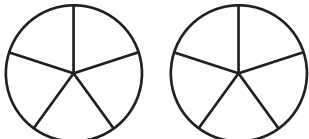
$\frac{5}{4}$ is the same as $1\frac{1}{4}$. So let's add the 1 to our answer of 10. Our answer is now $11\frac{1}{4}$.

- 4** Solve these problems, converting any improper fractions in your answer to mixed numerals. You can use the models to help you with the renaming:

a  $\frac{2}{3} + 2\frac{2}{3} = \boxed{2}\frac{\boxed{4}}{\boxed{3}}$ which is equivalent to $\boxed{3}\frac{\boxed{1}}{\boxed{3}}$

b  $3\frac{2}{4} + 1\frac{3}{4} = \boxed{4}\frac{\boxed{5}}{\boxed{4}}$ which is equivalent to $\boxed{5}\frac{\boxed{1}}{\boxed{4}}$

c  $7\frac{6}{8} + \frac{5}{8} = \boxed{7}\frac{\boxed{11}}{\boxed{8}}$ which is equivalent to $\boxed{8}\frac{\boxed{3}}{\boxed{8}}$

d  $3\frac{3}{5} + 16\frac{3}{5} = \boxed{19}\frac{\boxed{6}}{\boxed{5}}$ which is equivalent to $\boxed{20}\frac{\boxed{1}}{\boxed{5}}$

Sometimes we also come across more complicated subtraction problems.

Look at $1\frac{1}{4} - \frac{3}{4}$. We can't take away $\frac{3}{4}$ from $\frac{1}{4}$ so we will need to rename.

$1\frac{1}{4}$ is the same as $\frac{5}{4}$. $\frac{5}{4} - \frac{3}{4} = \frac{2}{4}$

- 5** Use renaming to solve these problems. Convert your answers to mixed numbers. You can draw models if that helps:

a $1\frac{2}{5} - \frac{4}{5} =$
 $\boxed{7}\frac{\boxed{4}}{\boxed{5}} - \frac{\boxed{4}}{\boxed{5}} = \frac{\boxed{3}}{\boxed{5}}$

b $2\frac{2}{4} - \frac{3}{4} =$
 $\boxed{10}\frac{\boxed{3}}{\boxed{4}} - \frac{\boxed{3}}{\boxed{4}} = \frac{\boxed{7}}{\boxed{4}}$
 $= \boxed{1}\frac{\boxed{3}}{\boxed{4}}$

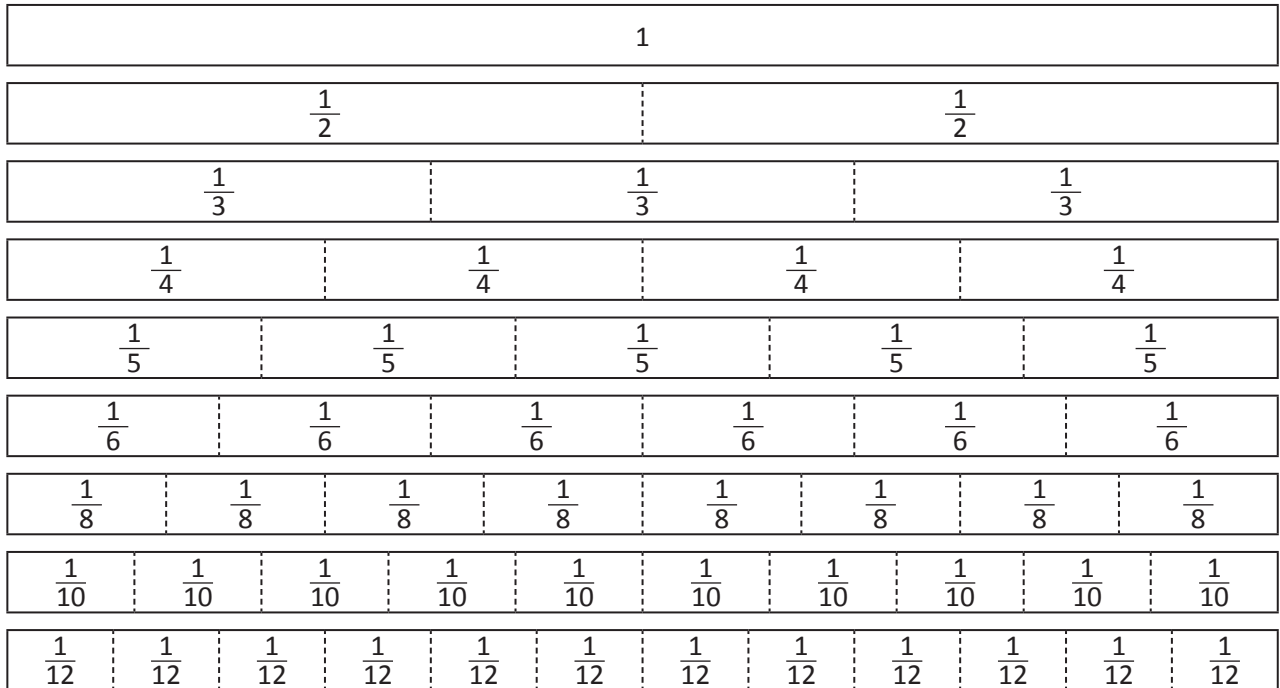
c $3\frac{2}{5} - \frac{4}{5} =$
 $\boxed{17}\frac{\boxed{4}}{\boxed{5}} - \frac{\boxed{4}}{\boxed{5}} = \frac{\boxed{13}}{\boxed{5}}$
 $= \boxed{2}\frac{\boxed{3}}{\boxed{5}}$

Calculating – adding and subtracting common fractions

Sometimes we need to add and subtract fractions that have different but related denominators.

Look at $\frac{3}{4} + \frac{1}{8}$ How do we do this? One way is to use fraction strips to find equivalent fractions.

We can see that $\frac{3}{4}$ is the same as $\frac{6}{8}$ $\frac{6}{8} + \frac{1}{8} = \frac{7}{8}$



6 Use the fraction strips above to help you add or subtract the like fractions. Rename the fractions in bold:

a $\frac{1}{4} + \frac{1}{2}$

1	2	3
4	4	4

b $\frac{2}{5} + \frac{6}{10}$

4	6	10
10	10	10

c $\frac{4}{5} - \frac{2}{10}$

8	2	6
10	10	10

d $\frac{4}{6} + \frac{2}{3}$

4	4	8
6	6	6

e $\frac{3}{4} - \frac{1}{2}$

3	2	1
4	4	4

f $\frac{3}{4} + \frac{1}{8}$

6	1	7
8	8	8

g Brad ate $\frac{2}{6}$ of a packet of chips. Jen ate $\frac{2}{3}$ of a packet of chips. How much did they eat altogether?

$$\frac{2}{6} + \frac{2}{3} = \frac{2}{6} + \frac{4}{6} = \frac{6}{6} = 1 \text{ packet}$$

h Write a problem for a partner to solve:

Answers will vary.

Calculating – multiplying fractions by whole numbers

We can use repeated addition to multiply fractions by whole numbers.

$$3 \times \frac{2}{8} \longrightarrow 3 \text{ lots of two eighths is } \frac{2}{8} + \frac{2}{8} + \frac{2}{8} = \frac{6}{8}$$

$$3 \times \frac{2}{8} = \frac{6}{8}$$

1 Use repeated addition to multiply these fractions. Show each of the steps:

a $3 \times \frac{3}{12}$

$$= \frac{3}{12} + \frac{3}{12} + \frac{3}{12}$$

$$= \frac{\boxed{9}}{\boxed{12}}$$

b $3 \times \frac{2}{7}$

$$= \frac{2}{7} + \frac{2}{7} + \frac{2}{7}$$

$$= \frac{6}{7}$$

c $5 \times \frac{1}{8}$

$$= \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$$

$$= \frac{5}{8}$$

d $3 \times \frac{2}{9}$

$$= \frac{2}{9} + \frac{2}{9} + \frac{2}{9}$$

$$= \frac{6}{9}$$

2 Try these. Convert your answers to whole numbers:

a $6 \times \frac{1}{2}$

$$= \frac{6}{2}$$

$$= 3$$

b $5 \times \frac{2}{5}$

$$= \frac{10}{5}$$

$$= 2$$

c $8 \times \frac{2}{4}$

$$= \frac{16}{4}$$

$$= 4$$

d $15 \times \frac{3}{5}$

$$= \frac{45}{5}$$

$$= 9$$

3 Sam thinks that $6 \times \frac{2}{6}$ is the same as $5 \times \frac{2}{5}$. Is he right? Show how you know:

$$6 \times \frac{2}{6}$$

$$= \frac{2}{6} + \frac{2}{6} + \frac{2}{6} + \frac{2}{6} + \frac{2}{6} + \frac{2}{6}$$

$$= \frac{12}{6} = 2$$

$$5 \times \frac{2}{5}$$

$$= \frac{2}{5} + \frac{2}{5} + \frac{2}{5} + \frac{2}{5} + \frac{2}{5}$$

$$= \frac{10}{5} = 2$$

Yes, they are the same.

4 Sam's dad helped him with his homework. And we all know how that works out ... Here is what his dad did. Is he right? If not, explain to him where he went wrong.

$$3 \times \frac{3}{8}$$

$$\frac{3}{8} + \frac{3}{8} + \frac{3}{8} = \frac{9}{24}$$

$$3 \times \frac{3}{8} = \frac{9}{24}$$

He must not add denominators.

$$3 \times \frac{3}{8}$$

$$= \frac{9}{8}$$

$$= 1\frac{1}{8}$$

Calculating – multiplying fractions by whole numbers

There is another way to multiply fractions by whole numbers. Look at $3 \times \frac{3}{5}$.

We have 3 lots of three fifths. We can express this as $\frac{3 \times 3}{5} = \frac{9}{5}$

We don't multiply the fifths because these don't change – we still have fifths.

5 Multiply these fractions by whole numbers. Express the answers as improper fractions:

a $4 \times \frac{3}{4}$

$$\frac{\boxed{4} \times \boxed{3}}{\boxed{4}} = \frac{\boxed{12}}{\boxed{4}}$$

b $4 \times \frac{2}{3}$

$$\frac{\boxed{4} \times \boxed{2}}{\boxed{3}} = \frac{\boxed{8}}{\boxed{3}}$$

c $5 \times \frac{2}{4}$

$$\frac{\boxed{5} \times \boxed{2}}{\boxed{4}} = \frac{\boxed{10}}{\boxed{4}}$$

d $3 \times \frac{3}{6}$

$$\frac{\boxed{3} \times \boxed{3}}{\boxed{6}} = \frac{\boxed{9}}{\boxed{6}}$$

e $2 \times \frac{4}{5}$

$$\frac{\boxed{2} \times \boxed{4}}{\boxed{5}} = \frac{\boxed{8}}{\boxed{5}}$$

f $5 \times \frac{2}{3}$

$$\frac{\boxed{5} \times \boxed{2}}{\boxed{3}} = \frac{\boxed{10}}{\boxed{3}}$$

Our answers are all improper fractions. How do we convert these to mixed numerals?

Look at $\frac{9}{4}$. This is nine quarters.

To change this to a mixed numeral we divide the numerator by the denominator:

$9 \div 4 = 2$ with 1 quarter left over. $\frac{9}{4}$ is the same as $2\frac{1}{4}$.

6 Warm up with these problems. There will be no remainders.

a $\frac{8}{4}$

$$\boxed{8} \div \boxed{4} = \boxed{2}$$

b $\frac{9}{3}$

$$\boxed{9} \div \boxed{3} = \boxed{3}$$

c $\frac{12}{6}$

$$\boxed{12} \div \boxed{6} = \boxed{2}$$

d $\frac{15}{5}$

$$\boxed{15} \div \boxed{5} = \boxed{3}$$

e $\frac{16}{4}$

$$\boxed{16} \div \boxed{4} = \boxed{4}$$

f $\frac{14}{7}$

$$\boxed{14} \div \boxed{7} = \boxed{2}$$

g $\frac{8}{2}$

$$\boxed{8} \div \boxed{2} = \boxed{4}$$

h $\frac{10}{5}$

$$\boxed{10} \div \boxed{5} = \boxed{2}$$

7 Now take your answers from Question 5 and write them here. Divide the numerators by the denominators to find their mixed numeral equivalents:

a $\frac{\boxed{12}}{\boxed{4}} = \boxed{3}$

b $\frac{\boxed{8}}{\boxed{3}} = \boxed{2} \frac{\boxed{2}}{\boxed{3}}$

c $\frac{\boxed{10}}{\boxed{4}} = \boxed{2} \frac{\boxed{2}}{\boxed{4}}$

d $\frac{\boxed{9}}{\boxed{6}} = \boxed{1} \frac{\boxed{3}}{\boxed{6}}$

e $\frac{\boxed{8}}{\boxed{5}} = \boxed{1} \frac{\boxed{3}}{\boxed{5}}$

f $\frac{\boxed{10}}{\boxed{3}} = \boxed{3} \frac{\boxed{1}}{\boxed{3}}$

Calculating – adding decimal fractions

How do we add decimal fractions using a written strategy?

We arrange the numbers so the place values line up and then we start with the smallest value.

We first add the tenths. 9 tenths and 4 tenths is 13 tenths.

We rename this as 1 unit and 3 tenths.

We write the 3 in the tenths column and move the unit to the units column.

Then we add the units. $1 + 4 + 6 = 11$

Don't forget the decimal point in your answer!

$$\begin{array}{r} 4 \ . \ 9 \\ + 6 \ . \ 4 \\ \hline 1 \ 1 \ . \ 3 \end{array}$$

1 Add these decimal numbers. The first one has been done for you.

a

$$\begin{array}{r} 4 \ 2 \ . \ 3 \\ + 3 \ 4 \ . \ 4 \\ \hline 7 \ 6 \ . \ 7 \end{array}$$

b

$$\begin{array}{r} 8 \ 4 \ . \ 2 \\ + 3 \ 4 \ . \ 6 \\ \hline 1 \ 1 \ 8 \ . \ 8 \end{array}$$

c

$$\begin{array}{r} 6 \ 0 \ . \ 4 \\ + 2 \ 5 \ . \ 1 \\ \hline 8 \ 5 \ . \ 5 \end{array}$$

d

$$\begin{array}{r} 3 \ . \ 0 \ 7 \\ + 9 \ . \ 2 \\ \hline 1 \ 2 \ . \ 2 \ 7 \end{array}$$

e

$$\begin{array}{r} 4 \ . \ 1 \\ + 3 \ . \ 4 \ 4 \\ \hline 7 \ . \ 5 \ 4 \end{array}$$

f

$$\begin{array}{r} 7 \ . \ 0 \ 2 \\ + 1 \ . \ 8 \ 7 \\ \hline 8 \ . \ 8 \ 9 \end{array}$$

g

$$\begin{array}{r} 4 \ 7 \ . \ 2 \\ + 2 \ 6 \ . \ 0 \ 7 \\ \hline 7 \ 3 \ . \ 2 \ 7 \end{array}$$

h

$$\begin{array}{r} 4 \ 5 \ . \ 7 \ 1 \\ + 3 \ 1 \ . \ 3 \ 4 \\ \hline 7 \ 7 \ . \ 0 \ 5 \end{array}$$

i

$$\begin{array}{r} 6 \ 4 \ . \ 2 \ 3 \\ + 1 \ 0 \ . \ 4 \\ \hline 7 \ 4 \ . \ 6 \ 3 \end{array}$$

2 We use the same process when adding more than two numbers. Add these bills:

1 cola.....	\$2.80
1 lime milkshake.....	\$3.25
4 dim sims.....	\$4.80
3 crab cakes.....	\$2.60
Total	\$13.45

1 child's entry ticket.....	\$15.60
1 disposable camera.....	\$ 7.95
3 fridge magnets.....	\$15.45
1 t-shirt – medium.....	\$22.99
Total	\$61.99

Calculating – adding decimal fractions

3 Use a mental or written strategy of your choice to solve these problems:

a Add 16.05 and 5.64

21.69

b Add 122.54 and 47.12

169.66

c Bob decided it was time to drop some weight before the big game. He lost 3.63 kg in the first week and 1.25 kg in the 2nd week. How much weight did he lose altogether?

4.88 kg

d Kate spent \$13.65 at one shop, \$4.59 at the second, and \$17.35 at the third. How much did she spend altogether?

\$35.59

We can also use our mental addition strategies when adding decimal fractions.



REMEMBER

4 Use a mental or written strategy of your choice to complete these magic number squares. Remember in magic number squares, each row, column and diagonal adds to give the magic number. Your knowledge of inverse operations will come in handy.

The magic number is 4.5

1.2	0.9	2.4
2.7	1.5	0.3
0.6	2.1	1.8

The magic number is 6.0

3.2	0.4	2.4
1.2	2.0	2.8
1.6	3.6	0.8

The magic number is 1.5

0.2	0.9	0.4
0.7	0.5	0.3
0.6	0.1	0.8

Use this space for any working out:

Calculating – subtracting decimal fractions

How do we subtract decimal fractions using a written strategy?

We arrange the numbers so the place values line up and then we start with the smallest value.

We first subtract the tenths. We have 4 tenths, can we subtract 5 tenths?

No, so we rename a unit as 10 tenths. Now we have 14 tenths. 14 tenths subtract 5 tenths is 9 tenths.

We have 5 units, can we takeaway 3 units? Yes, the answer is 2.

$$\begin{array}{r} 5\cancel{6} . 14 \\ - 3 . 5 \\ \hline 2 . 9 \end{array}$$

1 Solve these problems:

a
$$\begin{array}{r} 3\cancel{4} . 12 . 5 \\ - 3 . 4 . 4 \\ \hline 8 . 1 \end{array}$$

b
$$\begin{array}{r} 8 . 5\cancel{6} . 12 \\ - 3 . 4 . 6 \\ \hline 5 . 1 . 6 \end{array}$$

c
$$\begin{array}{r} 3 . 2 . 7 \\ - 2 . 0 . 4 \\ \hline 1 . 2 . 3 \end{array}$$

d
$$\begin{array}{r} 7 . 3\cancel{4} . 10 \\ - 5 . 2 . 5 \\ \hline 2 . 1 . 5 \end{array}$$

e
$$\begin{array}{r} 2 . 4 . 7 \\ - 2 . 1 . 5 \\ \hline 0 . 3 . 2 \end{array}$$

f
$$\begin{array}{r} 6 . 7 . 2 \\ - 4 . 5 . 1 \\ \hline 2 . 2 . 1 \end{array}$$

g
$$\begin{array}{r} 3 . 2 . 8 . 5 \\ - 2 . 1 . 6 . 3 \\ \hline 1 . 1 . 2 . 2 \end{array}$$

h
$$\begin{array}{r} 7 . 4 . 1 . 4 \\ - 1 . 2 . 0 . 1 \\ \hline 6 . 2 . 1 . 3 \end{array}$$

i
$$\begin{array}{r} 7 . 6 . 2\cancel{3} . 13 \\ - 2 . 0 . 2 . 5 \\ \hline 5 . 6 . 0 . 8 \end{array}$$

Sometimes we have to work with numbers that have a different amount of digits such as $8.4 - 5.35$. When this happens, we rename. 4 tenths becomes 40 hundredths: $8.40 - 5.35$

2 Rename these problems and solve:

a
$$\begin{array}{r} 1 . 6 . 4\cancel{5} . 10 \\ - 3 . 3 . 8 \\ \hline 1 . 3 . 1 . 2 \end{array}$$

b
$$\begin{array}{r} 6\cancel{7} . 11 . 7 \\ - 3 . 4 . 0 \\ \hline 3 . 7 . 7 \end{array}$$

c
$$\begin{array}{r} 8 . 8\cancel{9} . 11\cancel{2} . 10 \\ - 4 . 7 . 2 \\ \hline 8 . 4 . 4 . 8 \end{array}$$

Calculating – subtracting decimal fractions

3 Use a mental or written strategy of your choice to solve these problems:

We can also use our mental strategies when subtracting decimal fractions.



a $125.47 - 9.08$

116.39

b $24.75 - 8.35$

16.4

c Donny spent \$25.50 on a new memory card for his phone. The next day it appeared on special for \$17.95. If he had waited another day, how much would he have saved?

\$7.55

d Natasha buys *Complete Girl* at \$4.95 an issue. Her sister Nina buys *Dolly* at \$5.70 an issue. How much more does Nina spend?

\$0.75

4 Find the answers to these problems and solve the riddle: *Why did the man freeze his money?*

$\frac{H}{7.7}$	$\frac{E}{19.9}$	$\frac{W}{36.41}$	$\frac{A}{11.5}$	$\frac{N}{142.4}$	$\frac{T}{13.05}$	$\frac{E}{19.9}$	$\frac{D}{27.4}$	$\frac{C}{10.32}$	$\frac{O}{17.93}$	$\frac{L}{10.3}$	$\frac{D}{27.4}$
-----------------	------------------	-------------------	------------------	-------------------	-------------------	------------------	------------------	-------------------	-------------------	------------------	------------------

$\frac{H}{7.7}$	$\frac{A}{11.5}$	$\frac{R}{17.4}$	$\frac{D}{27.4}$	$\frac{C}{10.32}$	$\frac{A}{11.5}$	$\frac{S}{14.77}$	$\frac{H}{7.7}$
-----------------	------------------	------------------	------------------	-------------------	------------------	-------------------	-----------------

A $7.2 + 4.3$

W $25.29 + 11.12$

S $5.63 + 9.14$

O $13.4 + 4.53$

L $5.1 + 5.2$

H $3.4 + 4.3$

T $5.16 + 7.89$

E $13.4 + 6.5$

C $2.16 + 8.16$

N $69.3 + 73.1$

D $13.5 + 13.9$

R $9.85 + 7.55$

Calculating – multiplying decimals by 10, 100 and 1 000

When we multiply by 10 the number becomes larger by 1 place value.

When we multiply by 100 the number becomes larger by 2 place values.

When we multiply by 1 000 the number becomes larger by 3 place values.

Look what happens to 45.216 when we apply these rules:

$$45.216 \times 10 = 452.16$$

$$45.216 \times 100 = 4521.6$$

$$45.216 \times 1\,000 = 45\,216$$

- 1 Warm up with these. Work with a partner and a calculator. Predict your answers to the following then try out the problems. Your answers will be one or more of the following. The first one has been done for you.**

tens

tenths

hundredths

units

What place values are in your answers? Multiply by 10:

a these units: 6, 3, 1 *We get 60, 30, 10 (tens)*

b these tenths: 0.6, 0.3 and 0.1 *We get 6, 3, 1 (units)*

c these hundredths: 0.06, 0.03 and 0.01 *We get 0.6, 0.3, 0.1 (tenths)*

d these units and tenths: 1.6, 2.3 and 3.4 *We get 16, 23, 34 (tens and units)*

e these tenths and hundredths: 0.16, 0.23, 0.31 and 0.49 .. *We get 1.6, 2.3, 3.1, 4.9 (units and tenths)*

- 2 Multiply these decimals by 10, 100 and 1000. Estimate first.**

	$\times 10$	$\times 100$	$\times 1\,000$
0.5	5	50	500
0.25	2.5	25	250
0.37	3.7	37	370
1.2	12	120	1200
7.34	73.4	734	7340

- 3 Estimate, then calculate the answers:**

a $10 \times 0.7 =$ 7

b $100 \times 0.9 =$ 90

c $10 \times 0.3 =$ 3

d $100 \times 0.15 =$ 15

e $1000 \times 0.27 =$ 270

f $100 \times 0.45 =$ 45

g $100 \times 0.255 =$ 25.5

h $10 \times 0.555 =$ 5.55

i $1000 \times 0.178 =$ 178

Calculating – dividing decimals by 10, 100 and 1000

When we divide by 10 the number becomes smaller by 1 place value.

When we divide by 100 the number becomes smaller by 2 place values.

When we divide by 1000 the number becomes smaller by 3 place values.

Look what happens to 45 when we apply these rules:

$$45 \div 10 = 4.5$$

$$45 \div 100 = 0.45$$

$$45 \div 1000 = 0.045$$

1 Divide these numbers by 10, 100 and 1000. Estimate first.

	$\div 10$	$\div 100$	$\div 1000$
50	5	0.5	0.05
25	2.5	0.25	0.025
37.2	3.72	0.372	0.0372
48.5	4.85	0.485	0.0485
542	54.2	5.42	0.542

2 Estimate, then calculate the answers:

a $72 \div 10 =$

b $48 \div 1000 =$

c $35.2 \div 100 =$

d $92.05 \div 10 =$

e $345.7 \div 1000 =$

f $55.07 \div 100 =$

3 You'll work with a partner for this activity. You'll also need a calculator. Take turns giving each other a decimal number to transform.

- Give them the starting number and the number you want it to become.
- Your partner then has to do so in one move on the calculator, dividing by either 10, 100 or 1000.
- If they can do so, they score 10 points. If they get it wrong, you score 10 points. If you give them a problem that can't be solved by dividing by 10, 100 or 1000, they score the 10 points.
- Swap roles. First person to 50 points wins. Record the numbers below:

Answers will vary.

OK, start with 163. Turn it into 1.63 in 1 move.



Calculating – multiplying decimal fractions

How do we multiply decimal fractions using a written strategy?

First we estimate: $5 \times 3 = 15$. Our answer will be around 15.

3×5 tenths is 15 tenths. We rename this as 1 unit and 5 tenths.

We write the 5 in the tenths column and move the unit to the units column.

3×4 is 12. We also add the 1.

$3 \times 4.5 = 13.5$

We check the answer against our estimate. Do they fit?

$$\begin{array}{r} ^1 4 . 5 \\ \times 3 \\ \hline 1 3 . 5 \\ \hline \end{array}$$

1 Multiply these decimal fractions:

a $\begin{array}{r} ^1 2 . 6 \\ \times 2 \\ \hline 5 . 2 \\ \hline \end{array}$

b $\begin{array}{r} ^2 3 . 7 \\ \times 4 \\ \hline 1 4 . 8 \\ \hline \end{array}$

c $\begin{array}{r} ^1 5 . 2 \\ \times 5 \\ \hline 2 6 . 0 \\ \hline \end{array}$

d $\begin{array}{r} ^3 8 . 4 \\ \times 8 \\ \hline 6 7 . 2 \\ \hline \end{array}$

e $\begin{array}{r} ^1 1 ^1 4 . 5 \\ \times 3 \\ \hline 4 3 . 5 \\ \hline \end{array}$

f $\begin{array}{r} ^3 2 ^3 4 . 5 \\ \times 7 \\ \hline 1 7 1 . 5 \\ \hline \end{array}$

2 Now try these:

a $\begin{array}{r} 3 . ^1 2 3 \\ \times 4 \\ \hline 1 2 . 9 2 \\ \hline \end{array}$

b $\begin{array}{r} 5 . 3 3 \\ \times 3 \\ \hline 1 5 . 9 9 \\ \hline \end{array}$

c $\begin{array}{r} ^3 8 . ^1 4 2 \\ \times 8 \\ \hline 6 7 . 3 6 \\ \hline \end{array}$

d $\begin{array}{r} ^2 7 . ^2 4 4 \\ \times 6 \\ \hline 4 4 . 6 4 \\ \hline \end{array}$

e $\begin{array}{r} ^1 6 . ^3 2 8 \\ \times 4 \\ \hline 2 5 . 1 2 \\ \hline \end{array}$

f $\begin{array}{r} ^3 3 . ^4 4 5 \\ \times 8 \\ \hline 2 7 . 6 0 \\ \hline \end{array}$

3 Use the templates to set up and solve these money problems:

- a Yasmin buys 3 cartons of choc milk. Each carton costs \$2.45. How much money does she spend?

$$\begin{array}{r} ^1 2 . ^1 4 5 \\ \times 3 \\ \hline \$ 7 . 3 5 \\ \hline \end{array}$$

- b Lisa buys 4 magazines. Each magazine costs \$4.95. How much does she spend on magazines in total?

$$\begin{array}{r} ^3 4 . ^2 9 5 \\ \times 4 \\ \hline \$ 1 9 . 8 0 \\ \hline \end{array}$$

- c Omar wants to buy 3 games for his computer. Each game is \$14.95. He has saved \$45. Does he have enough money?

$$\begin{array}{r} ^1 1 ^2 4 . ^1 9 5 \\ \times 3 \\ \hline \$ 4 4 . 8 5 \\ \hline \end{array}$$

Yes

Calculating – multiplying decimal fractions

We can also use renaming to multiply decimal fractions. Look at 4×3.6 :

$$\begin{array}{r} ^2 3 6 \\ \times 4 \\ \hline 1 4 4 \text{ tenths} \end{array}$$

3.6 can also be expressed as 36 tenths.

$$36 \times 4 = 144$$

Then we convert back to decimals:

144 tenths is 14.4

4 Rename these decimal fractions then multiply. The first one has been started for you.

a $3 \times 2.7 = \boxed{8.1}$

2.7 is 27 tenths

$$\begin{array}{r} ^2 2 7 \\ \times 3 \\ \hline 8 1 \end{array}$$

$$3 \times 2.7 = \underline{8.1}$$

b $5 \times 3.4 = \boxed{17.0}$

3.4 is 34 tenths

$$\begin{array}{r} ^2 3 4 \\ \times 5 \\ \hline 1 7 0 \end{array}$$

$$5 \times 3.4 = 17.0$$

c $4 \times 9.7 = \boxed{38.8}$

9.7 is 97 tenths

$$\begin{array}{r} ^2 9 7 \\ \times 4 \\ \hline 3 8 8 \end{array}$$

$$4 \times 9.7 = 38.8$$

d $7 \times 1.9 = \boxed{13.3}$

1.9 is 19 tenths

$$\begin{array}{r} ^6 1 9 \\ \times 7 \\ \hline 1 3 3 \end{array}$$

$$7 \times 1.9 = 13.3$$

5 Try these. These numbers have hundredths so we will rename the decimal fractions as hundredths. The first one has been done for you.

a $4 \times 6.12 = \boxed{24.48}$

6.12 is 612 hths

$$\begin{array}{r} ^6 ^1 ^2 6 1 2 \\ \times 4 \\ \hline 2 4 4 8 \end{array}$$

$$4 \times 6.12 = 24.48$$

b $5 \times 3.42 = \boxed{17.1}$

3.42 is 342 hths

$$\begin{array}{r} ^2 ^1 3 ^1 4 ^2 3 4 2 \\ \times 5 \\ \hline 1 7 1 0 \end{array}$$

$$5 \times 3.42 = 17.1$$

c $4 \times 9.73 = \boxed{38.92}$

9.73 is 973 hths

$$\begin{array}{r} ^2 ^1 9 ^1 7 ^3 3 7 3 \\ \times 4 \\ \hline 3 8 9 2 \end{array}$$

$$4 \times 9.73 = 38.92$$

d $7 \times 1.94 = \boxed{13.58}$

1.94 is 194 hths

$$\begin{array}{r} ^6 ^2 ^9 1 ^2 9 ^4 1 9 4 \\ \times 7 \\ \hline 1 3 5 8 \end{array}$$

$$7 \times 1.94 = 13.58$$

6 Solve these problems:

- a Danielle and her twin brothers are each 1.57 m tall. What is their combined height?

$$4.71 \text{ m}$$

- b Your favourite cereal is on special for \$4.55 per box. You wait until your mum is in a weakened state and then masterfully convince her that buying 7 boxes is a great idea. How much will this cost?

$$\$31.85$$

Unless there's a zero at the end, if I multiply tenths, I will always have tenths in my answer. If I multiply by hundredths, I'll always have hundredths in my answer. It's a good way to check that my answers are right.



Calculating – multiplying decimal fractions

- 7 You and your friends are going to the movies and it's your shout. Look at the price list below and use a multiplication strategy of your choice to answer the following questions. Show your thinking:

- a How much will it cost you for 4 "Under 13" tickets?

\$42.00

- b Two of your friends each want a large drink and a medium popcorn. What will that cost you?

\$14.00



Ticket prices	
Under 13	\$10.50
Adult	\$14.50
Refreshments	
Popcorn	S \$2.50
	M \$3.50
	L \$4.50
Drink	S \$2.50
	M \$3.00
	L \$3.50
Chocolate bar	\$1.95
Choc top	\$3.25
Water	\$1.95
Chips/Crisps	\$2.95

- c You and your other friend want a choc top and a large drink each. What will that cost?

\$13.50

- d Halfway through the movie, you are all dying of thirst and you go out and buy 4 bottles of water. You pay for them with a \$20 note. How much change do you receive?

\$12.20

- e Use the refreshment price list to design and calculate the cost of a snack that would help get you through this Maths lesson.

Answers will vary.

Which operations do I need to use here? Is it only multiplication?



Calculating – dividing decimal fractions

Look at 64.4 divided by 5. We start with the largest place value.

6 tens divided by 5 is 1 ten with a remainder of 1 ten.

We rename this as 10 units and carry it over to the units column.

14 units divided by 5 is 2 with 4 units left over.

We rename this as 40 tenths and carry it. We now have 44 tenths.

44 tenths divided by 5 is 8 with a remainder of 4. We rename this as

40 hundredths. 40 hundredths divided by 5 is 8.

64.4 divided by 5 is 12.88

$$\begin{array}{r} 12.88 \\ 5 \overline{) 64.40} \\ \underline{5} \\ 14 \\ \underline{10} \\ 44 \\ \underline{40} \\ 40 \\ \underline{40} \\ 0 \end{array}$$

1 Divide these:

a

$$\begin{array}{r} 10.7 \\ 8 \overline{) 85.6} \\ \underline{8} \\ 5 \\ \underline{4} \\ 15 \\ \underline{16} \\ 5 \\ \underline{4} \\ 10 \\ \underline{8} \\ 20 \\ \underline{16} \\ 40 \\ \underline{40} \\ 0 \end{array}$$

b

$$\begin{array}{r} 09.4 \\ 5 \overline{) 47.20} \\ \underline{4} \\ 7 \\ \underline{5} \\ 20 \\ \underline{10} \\ 10 \\ \underline{10} \\ 0 \end{array}$$

c

$$\begin{array}{r} 8.3 \\ 7 \overline{) 58.21} \\ \underline{7} \\ 58 \\ \underline{56} \\ 21 \\ \underline{21} \\ 0 \end{array}$$

d

$$\begin{array}{r} 12.7 \\ 5 \overline{) 63.5} \\ \underline{5} \\ 13 \\ \underline{10} \\ 35 \\ \underline{30} \\ 50 \\ \underline{50} \\ 0 \end{array}$$

e

$$\begin{array}{r} 19.8 \\ 5 \overline{) 99.40} \\ \underline{5} \\ 99 \\ \underline{95} \\ 40 \\ \underline{40} \\ 0 \end{array}$$

f

$$\begin{array}{r} 12.05 \\ 6 \overline{) 72.30} \\ \underline{6} \\ 12 \\ \underline{12} \\ 30 \\ \underline{30} \\ 0 \end{array}$$

2 Sharing money is a time when we divide decimal fractions. Add the bills then divide them evenly among 4 people. Don't listen to the guy who said he only ate the rice – he's a cheapskate.

2 hot chocolates.....	\$5.60
2 milkshakes.....	\$4.20
2 muffins.....	\$5.80
1 large bowl chips.....	\$4.60
Total	\$20.20

\$5.05

1 Pad Thai.....	\$ 9.50
1 king prawns with veg....	\$19.30
1 beef and broccoli.....	\$12.50
1 large rice.....	\$ 3.30
4 colas.....	\$ 8.60
Total	\$53.20

\$13.30

Calculating – dividing decimal fractions

3 Solve these decimal word problems using a mental or written strategy of your choice:

- a You and 6 friends win a jackpot totalling \$248.15. If you share the prize equally, how much will each of you receive?

$$\begin{array}{r} \$ \quad 248.15 \\ 7 \overline{) \$ \quad 248.15} \end{array}$$

- b Two of these friends decide that money is the root of all evil and forgo their share. How much do you each receive now?

$$\$248.15 \div 5 = \$49.63$$

- c You're thirsty from all the excitement, so you buy 5 bottles of water, costing a total of \$11.25. What was the cost of each bottle?

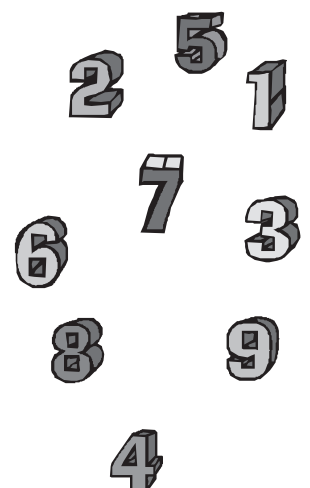
$$\begin{array}{r} \$ \quad 11.25 \\ 5 \overline{) \$ \quad 11.25} \end{array}$$

4 You remember the answer 6.125. But you have lost the question! You know it was a division problem and that you divided 2 whole numbers to get to the answer. Both the numbers were smaller than 60. But that's all you remember. And your teacher wants to see what you have been doing during the lesson.

Work out what the division problem was. You can try this with or without a calculator.

$$? \div ? = 6.125$$

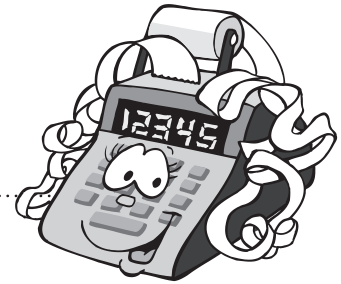
$$49 \div 8 = 6.125$$





Getting ready

See if you can guess the secret numbers below.
You can use a calculator and co-opt a partner if you like.



What to do

- 1 I start with the number. I halve it, add 3.6 to that answer, divide this new number by 4 and then I add 0.3. My answer is 6.5. What number did I start with?

42.4

- 2 I start with a new secret number. I add 1.4 to this, divide the new number by 11, halve the quotient and then halve it again. My answer is 1.25. What number did I start with?

53.6

- 3 I start with a number, then halve it. I subtract 18.05 from the answer and then multiply this number by 3. I add 6 to the total and my answer is 96.3. What number did I start with?

96.3

- 4 I start with a number and divide it by 8. I multiply the answer by 3.2 and then subtract 4.1 from this new answer. I multiply this by 23 and end up with 52.9. What number did I start with?

16

Work backwards! You have to do the opposite process for each step.



What to do next

Now you know how these work, can you write your own problem for a partner to solve?

Answers will vary.

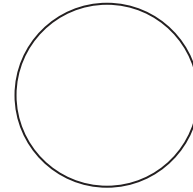


1 Divide and shade the objects to show the following equivalent fractions:

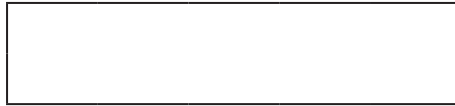
a $\frac{1}{2} = \frac{2}{4}$



b $\frac{1}{4} = \frac{2}{8}$



c $\frac{2}{5} = \frac{4}{10}$



2 Show the following equivalent fractions:

a $\frac{1}{3} = \frac{\square}{9}$

b $\frac{2}{4} = \frac{\square}{2}$

c $\frac{1}{4} = \frac{\square}{8}$

d $\frac{3}{4} = \frac{15}{\square}$

3 In each group, circle the equivalent fractions:

a $\frac{1}{2}$ $\frac{2}{5}$ $\frac{2}{4}$ $\frac{1}{3}$ $\frac{50}{100}$

b $\frac{2}{3}$ $\frac{4}{10}$ $\frac{1}{2}$ $\frac{2}{5}$ $\frac{40}{100}$

4 Find the highest common factor (HCF) for each pair:

a 16 8 \square

b 20 25 \square

c 24 18 \square

d 15 20 \square

5 Find the HCF then simplify these fractions to their lowest terms:

a $\frac{7}{14} = \frac{\square}{\square}$ HCF \square

b $\frac{10}{100} = \frac{\square}{\square}$ HCF \square

c $\frac{25}{100} = \frac{\square}{\square}$ HCF \square

d $\frac{12}{24} = \frac{\square}{\square}$ HCF \square

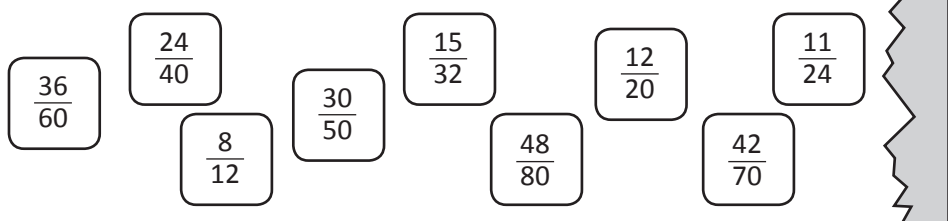
e $\frac{75}{100} = \frac{\square}{\square}$ HCF \square

f $\frac{35}{50} = \frac{\square}{\square}$ HCF \square

6 Make a path across the page by colouring any fractions that are equivalent to $\frac{6}{10}$:

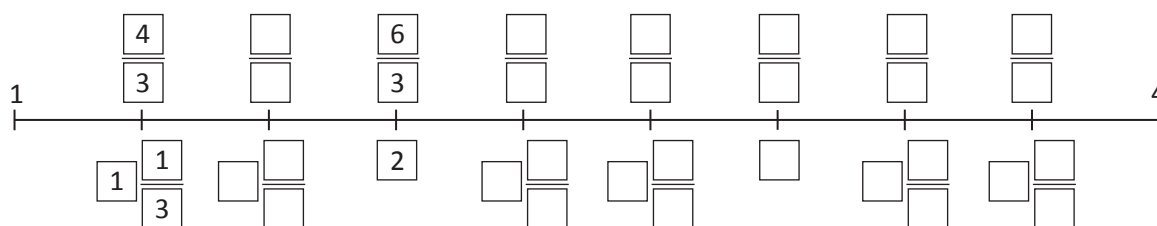


START



FINISH

7 Look carefully at the number line and fill in the missing information:



8 Write the matching improper fraction or mixed numeral for:

a $1\frac{1}{4} = \frac{\boxed{}}{\boxed{}}$

b $\frac{5}{2} = \boxed{}\frac{\boxed{}}{\boxed{}}$

c $1\frac{1}{3} = \frac{\boxed{}}{\boxed{}}$

d $\frac{8}{6} = \boxed{}\frac{\boxed{}}{\boxed{}}$

9 Order these fractions from smallest to largest. You may need to rename:

Working space

a $\frac{2}{5}$ $\frac{1}{5}$ $\frac{10}{5}$ $\frac{3}{5}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$

b $\frac{1}{4}$ $\frac{1}{2}$ $\frac{3}{8}$ $\frac{12}{16}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$

c $\frac{3}{8}$ $\frac{2}{4}$ $\frac{5}{6}$ $\frac{4}{24}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$ $\frac{\boxed{}}{\boxed{}}$

10 Write a fraction that is larger than the following. It must have a different denominator. It can have a different numerator:

a $\frac{1}{2}$ $\frac{\boxed{}}{\boxed{}}$

b $\frac{1}{4}$ $\frac{\boxed{}}{\boxed{}}$

c $\frac{2}{3}$ $\frac{\boxed{}}{\boxed{}}$

d $\frac{4}{5}$ $\frac{\boxed{}}{\boxed{}}$

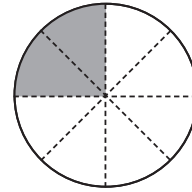
Skills	Not yet	Kind of	Got it
• Recognises, represents and creates equivalent fractions			
• Finds HCF for related numbers			
• Simplifies fractions to lowest common form			
• Matches improper fractions to mixed numerals			
• Converts between improper fractions and mixed numerals			
• Compares and orders fractions with like denominators			
• Compares and orders fractions with related denominators			

1 Divide and shade the objects to show the following equivalent fractions:

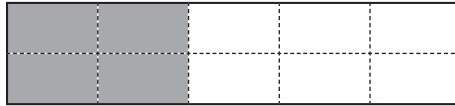
a $\frac{1}{2} = \frac{2}{4}$



b $\frac{1}{4} = \frac{2}{8}$



c $\frac{2}{5} = \frac{4}{10}$



2 Show the following equivalent fractions:

a $\frac{1}{3} = \frac{\boxed{3}}{9}$

b $\frac{2}{4} = \frac{\boxed{1}}{2}$

c $\frac{1}{4} = \frac{\boxed{2}}{8}$

d $\frac{3}{4} = \frac{15}{\boxed{20}}$

3 In each group, circle the equivalent fractions:

a $\frac{1}{2}$ $\frac{2}{5}$ $\frac{2}{4}$ $\frac{1}{3}$ $\frac{50}{100}$

b $\frac{2}{3}$ $\frac{4}{10}$ $\frac{1}{2}$ $\frac{2}{5}$ $\frac{40}{100}$

4 Find the highest common factor (HCF) for each pair:

a 16 8 $\boxed{8}$

b 20 25 $\boxed{5}$

c 24 18 $\boxed{6}$

d 15 20 $\boxed{5}$

5 Find the HCF then simplify these fractions to their lowest terms:

a $\frac{7}{14} = \frac{\boxed{1}}{\boxed{2}}$ HCF $\boxed{7}$

b $\frac{10}{100} = \frac{\boxed{1}}{\boxed{10}}$ HCF $\boxed{10}$

c $\frac{25}{100} = \frac{\boxed{1}}{\boxed{4}}$ HCF $\boxed{25}$

d $\frac{12}{24} = \frac{\boxed{1}}{\boxed{2}}$ HCF $\boxed{12}$

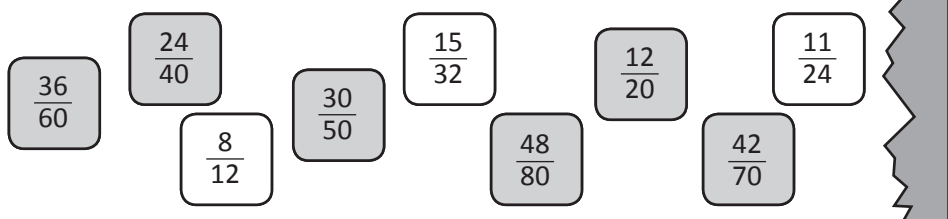
e $\frac{75}{100} = \frac{\boxed{3}}{\boxed{4}}$ HCF $\boxed{25}$

f $\frac{35}{50} = \frac{\boxed{7}}{\boxed{10}}$ HCF $\boxed{5}$

6 Make a path across the page by colouring any fractions that are equivalent to $\frac{6}{10}$:



START



FINISH

7 Look carefully at the number line and fill in the missing information:

1 4

4 5 6 7 8 9 10 11

3 3 3 3 3 3 3 3

1 1 2 2 2 3 3 3

a $1\frac{1}{4} = \frac{\boxed{5}}{\boxed{4}}$ **b** $\frac{5}{2} = \boxed{2}\frac{\boxed{1}}{\boxed{2}}$ **c** $1\frac{1}{3} = \frac{\boxed{4}}{\boxed{3}}$ **d** $\frac{8}{6} = \boxed{1}\frac{\boxed{2}}{\boxed{6}}$

a	$\frac{2}{5}$	$\frac{1}{5}$	$\frac{10}{5}$	$\frac{3}{5}$	$\frac{\boxed{1}}{\boxed{5}}$	$\frac{\boxed{2}}{\boxed{5}}$	$\frac{\boxed{3}}{\boxed{5}}$	$\frac{\boxed{10}}{\boxed{5}}$
b	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{3}{8}$	$\frac{12}{16}$	$\frac{\boxed{1}}{\boxed{4}}$	$\frac{\boxed{3}}{\boxed{8}}$	$\frac{\boxed{1}}{\boxed{2}}$	$\frac{\boxed{12}}{\boxed{16}}$
c	$\frac{3}{8}$	$\frac{2}{4}$	$\frac{5}{6}$	$\frac{4}{24}$	$\frac{\boxed{4}}{\boxed{24}}$	$\frac{\boxed{3}}{\boxed{8}}$	$\frac{\boxed{2}}{\boxed{4}}$	$\frac{\boxed{5}}{\boxed{6}}$

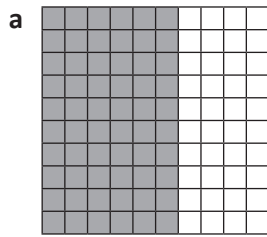
$$\begin{array}{cccc} \frac{4}{16} & \frac{8}{16} & \frac{6}{16} & \frac{12}{16} \\ \frac{9}{24} & \frac{12}{24} & \frac{20}{24} & \frac{4}{24} \end{array}$$

Answers will vary.

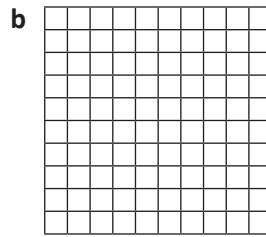
a $\frac{1}{2}$ $\frac{\square}{\square}$ **b** $\frac{1}{4}$ $\frac{\square}{\square}$ **c** $\frac{2}{3}$ $\frac{\square}{\square}$ **d** $\frac{4}{5}$ $\frac{\square}{\square}$

48 Series G Topic 1 Assessment

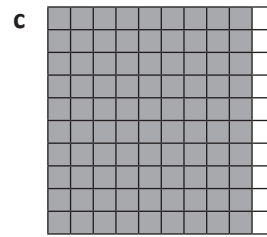
1 Fill in the missing information:



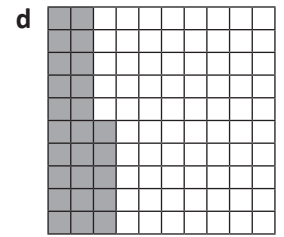
$\frac{60}{100}$	0.
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—	0.33
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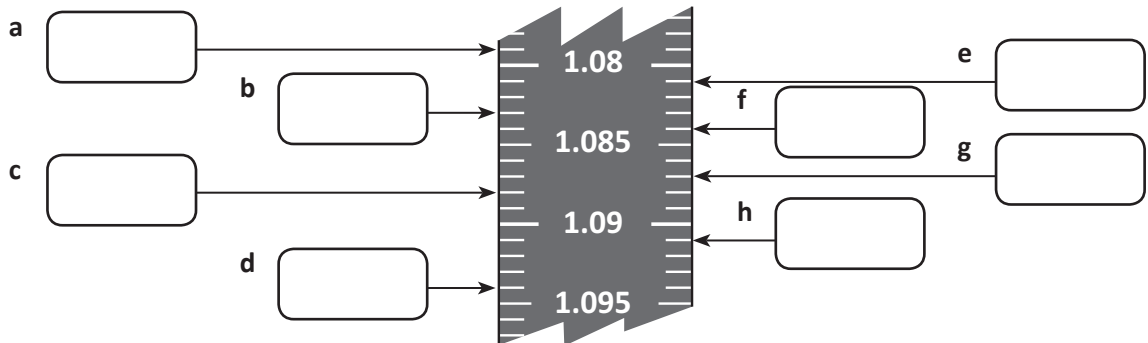


—	0.
---	----



—	0.
---	----

2 Look at this number line. Write what the numbers a to h represent:



3 Express these as decimal fractions:

a 4 tenths, 8 hundredths, 3 thousandths

.			
---	--	--	--

b $\frac{587}{1000}$

.			
---	--	--	--

c 5 units, 9 hundredths, 3 thousandths

.			
---	--	--	--

d 4 units, 8 tenths, 6 thousandths

.			
---	--	--	--

4 In each example find the value of the digit in bold. Write unit, tenth, hundredth or thousandth:

a 5.**8**2

--

b 63.**2**27

--

c 13.**0**53

--

d 124.**0**70

--

5 Circle the larger number:

a 4.098 4.980

b 13.352 1.3352

6 Look at the decimal number below. Write a decimal number that is smaller than it to the left. Write a decimal number that is greater than it to the right:

--

34.672

--

7 Fill in the missing information:

- a 43 hundredths is also tenths + hundredths
- b 99 hundredths is also tenths + hundredths
- c 0 tenths and 8 hundredths is also hundredths
- d 1 tenth and 6 hundredths is also hundredths
- e 7 tenths 6 hundredths and 8 thousandths is also thousandths
- f 433 thousandths is also tenths + hundredths + thousandths
- g 76 thousandths is also tenths + hundredths + thousandths

8 Round these numbers to the nearest tenth:

- a 67.23 _____ b 48.07 _____ c 124.78 _____ d 90.14 _____

9 Round these numbers to the nearest hundredth:

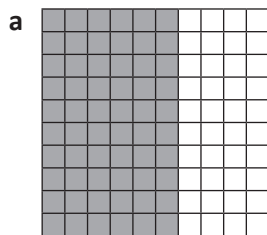
- a 58.127 _____ b 70.345 _____ c 45.007 _____ d 78.134 _____

10 Shade the following fractions and fill in the missing information:

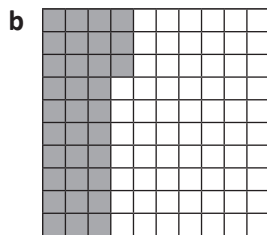
a		b		c		d	
	<input type="text"/> $\frac{1}{4}$ <input type="text"/> 0. <input type="text"/> %		<input type="text"/> $\frac{3}{4}$ <input type="text"/> 0. <input type="text"/> %		<input type="text"/> $\frac{1}{2}$ <input type="text"/> 0. <input type="text"/> %		<input type="text"/> $\frac{6}{10}$ <input type="text"/> 0. <input type="text"/> %

Skills	Not yet	Kind of	Got it
• Matches common fractions to decimal fractions			
• Places decimals (units, tenths and hundredths) on a number line			
• Identifies place value of numerals to 3 decimal places			
• Compares and orders decimals to 3 decimal places			
• Renames decimals			
• Rounds to the nearest tenth/hundredth			
• Recognises common percentages and relates to fractions			

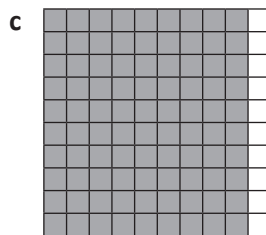
1 Fill in the missing information:



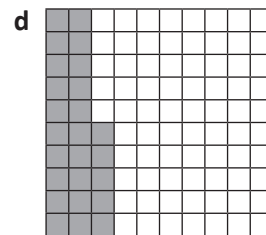
$\frac{60}{100}$	0.6(0)
------------------	--------



$\frac{33}{100}$	0.33
------------------	------

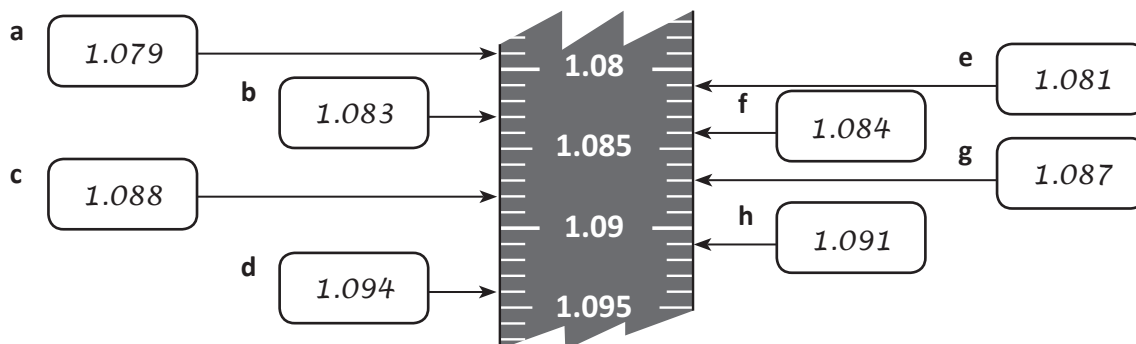


$\frac{90}{100}$	0.9(0)
------------------	--------



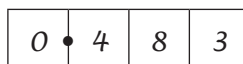
$\frac{25}{100}$	0.25
------------------	------

2 Look at this number line. Write what the numbers a to h represent:

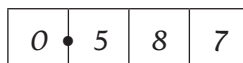


3 Express these as decimal fractions:

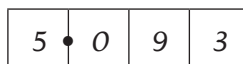
a 4 tenths, 8 hundredths, 3 thousandths



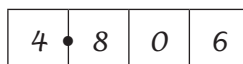
b $\frac{587}{1000}$



c 5 units, 9 hundredths, 3 thousandths



d 4 units, 8 tenths, 6 thousandths



4 In each example find the value of the digit in bold. Write unit, tenth, hundredth or thousandth:

a 5.**8**2

tenth

b 63.**2**27

thousandth

c 13.**0**53

hundredth

d 124.**0**70

hundredth

5 Circle the larger number:

a 4.098

4.980

b

13.352

1.3352

6 Look at the decimal number below. Write a decimal number that is smaller than it to the left. Write a decimal number that is greater than it to the right:

Answers will vary.

34.672

7 Fill in the missing information:

- a 43 hundredths is also 4 tenths + 3 hundredths
- b 99 hundredths is also 9 tenths + 9 hundredths
- c 0 tenths and 8 hundredths is also 8 hundredths
- d 1 tenth and 6 hundredths is also 16 hundredths
- e 7 tenths 6 hundredths and 8 thousandths is also 768 thousandths
- f 433 thousandths is also 4 tenths + 3 hundredths + 3 thousandths
- g 76 thousandths is also 0 tenths + 7 hundredths + 6 thousandths

8 Round these numbers to the nearest tenth:

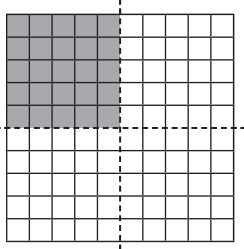
- a 67.23 67.2 b 48.07 48.1 c 124.78 124.8 d 90.14 90.1

9 Round these numbers to the nearest hundredth:

- a 58.127 58.13 b 70.345 70.35 c 45.007 45.01 d 78.134 78.13

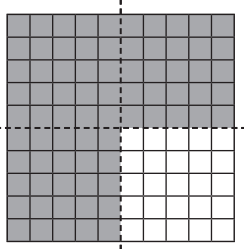
10 Shade the following fractions and fill in the missing information:

a



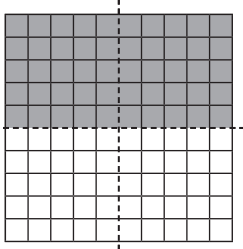
$\frac{1}{5}$	0.2	20%
---------------	-----	-----

b



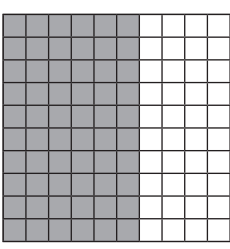
$\frac{7}{10}$	0.7	70%
----------------	-----	-----

c



$\frac{1}{2}$	0.5	50%
---------------	-----	-----

d



$\frac{3}{5}$	0.6	60%
---------------	-----	-----

Skills	Not yet	Kind of	Got it
• Matches common fractions to decimal fractions			
• Places decimals (units, tenths and hundredths) on a number line			
• Identifies place value of numerals to 3 decimal places			
• Compares and orders decimals to 3 decimal places			
• Renames decimals			
• Rounds to the nearest tenth/hundredth			
• Recognises common percentages and relates to fractions			

1 What is:

a $\frac{1}{4}$ of 16

b $\frac{1}{2}$ of 100

c $\frac{1}{3}$ of 90

d $\frac{1}{7}$ of 63

e $\frac{1}{4}$ of 200

f $\frac{1}{8}$ of 96

2 What is:

a $\frac{2}{3}$ of 15

b $\frac{3}{4}$ of 20

c $\frac{2}{8}$ of 24

d $\frac{3}{10}$ of 100

e $\frac{4}{10}$ of 80

f $\frac{7}{8}$ of 56

3 What is:

a 25% of 100

b 25% of 200

c 25% of 50

d 75% of 100

e 75% of 200

f 75% of 80

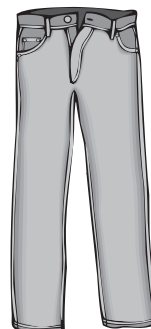
4 The following items are on special. Calculate the savings and the new price:



\$60 – 25% off

Saving _____

New price _____



\$50 – 10% off

Saving _____

New price _____



\$80 – 40% off

Saving _____

New price _____



\$80 – $\frac{2}{10}$ off

Saving _____

New price _____

Skills	Not yet	Kind of	Got it
• Finds unit fractions of amounts when answer is whole number			
• Finds fractions of amounts when answer is whole number			
• Finds percentages of amounts using patterns			
• Calculates discounts			

1 What is:

a $\frac{1}{4}$ of 16 4

b $\frac{1}{2}$ of 100 50

c $\frac{1}{3}$ of 90 30

d $\frac{1}{7}$ of 63 9

e $\frac{1}{4}$ of 200 50

f $\frac{1}{8}$ of 96 12

2 What is:

a $\frac{2}{3}$ of 15 10

b $\frac{3}{4}$ of 20 15

c $\frac{2}{8}$ of 24 6

d $\frac{3}{10}$ of 100 30

e $\frac{4}{10}$ of 80 32

f $\frac{7}{8}$ of 56 49

3 What is:

a 25% of 100 25

b 25% of 200 50

c 25% of 50 12.50

d 75% of 100 75

e 75% of 200 150

f 75% of 80 60

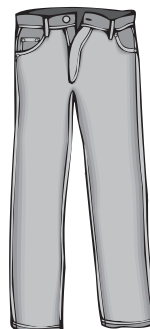
4 The following items are on special. Calculate the savings and the new price:



\$60 – 25% off

Saving \$15

New price \$45



\$50 – 10% off

Saving \$5

New price \$45



\$80 – 40% off

Saving \$32

New price \$48



\$80 – $\frac{2}{10}$ off

Saving \$16

New price \$64

Skills	Not yet	Kind of	Got it
• Finds unit fractions of amounts when answer is whole number			
• Finds fractions of amounts when answer is whole number			
• Finds percentages of amounts using patterns			
• Calculates discounts			

1 Solve these addition and subtraction problems:

a $\frac{1}{4} + \frac{2}{4} = \frac{\boxed{}}{\boxed{}}$

b $6\frac{1}{5} + 1\frac{3}{5} = \boxed{}\frac{\boxed{}}{\boxed{}}$

c $\frac{5}{8} - \frac{3}{8} = \frac{\boxed{}}{\boxed{}}$

d $3\frac{3}{12} - 1\frac{1}{12} = \boxed{}\frac{\boxed{}}{\boxed{}}$

2 Solve these problems. Show your working out:

a Lisa has $\frac{3}{4}$ of a packet of chocolate. Bart also has $\frac{3}{4}$ of a packet. How much chocolate do they have in total?

b Niah has $4\frac{3}{4}$ packets of cookies and gives $2\frac{1}{4}$ to her friend. How many is she left with?

c $\frac{2}{4} + \frac{3}{8} =$

d Achmed spends $\frac{3}{4}$ of an hour on Live Mathletics on Monday. On Tuesday, he spends $\frac{1}{2}$ an hour. Write the amount of time he has spent as a fraction:

What is this in minutes? _____

3 Use repeated addition to multiply these fractions. Express your answer as an improper fraction and as a mixed numeral if necessary:

a $3 \times \frac{1}{6} = \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$

b $2 \times \frac{5}{8} = \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}} = \boxed{}\frac{\boxed{}}{\boxed{}}$

c $3 \times \frac{3}{8} = \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}} = \boxed{}\frac{\boxed{}}{\boxed{}}$

d $4 \times \frac{5}{7} = \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} + \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}} = \boxed{}\frac{\boxed{}}{\boxed{}}$

4 Multiply these fractions. Express the answers as improper fractions:

a $3 \times \frac{3}{4}$
 $\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$

b $3 \times \frac{2}{4}$
 $\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$

c $5 \times \frac{3}{5}$
 $\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$

d $2 \times \frac{3}{6}$
 $\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}} = \frac{\boxed{}}{\boxed{}}$

5 Add these decimals:

a

$$\begin{array}{r} 42.5 \\ + 34.4 \\ \hline \\ \hline \end{array}$$

b

$$\begin{array}{r} 84.5 \\ + 37.6 \\ \hline \\ \hline \end{array}$$

c

$$\begin{array}{r} 60.42 \\ + 25.9 \\ \hline \\ \hline \end{array}$$

d

$$\begin{array}{r} 3.074 \\ + 9.262 \\ \hline \\ \hline \end{array}$$

e

$$\begin{array}{r} 4.15 \\ + 3.4 \\ \hline \\ \hline \end{array}$$

f

$$\begin{array}{r} 7.042 \\ + 1.87 \\ \hline \\ \hline \end{array}$$

6 Subtract these decimals:

a

$$\begin{array}{r} 55.3 \\ - 41.2 \\ \hline \\ \hline \end{array}$$

b

$$\begin{array}{r} 56.3 \\ - 24.6 \\ \hline \\ \hline \end{array}$$

c

$$\begin{array}{r} 51.63 \\ - 34.78 \\ \hline \\ \hline \end{array}$$

d

$$\begin{array}{r} 6.354 \\ - 4.06 \\ \hline \\ \hline \end{array}$$

e

$$\begin{array}{r} 3.167 \\ - 2.383 \\ \hline \\ \hline \end{array}$$

f

$$\begin{array}{r} 8.031 \\ - 7.174 \\ \hline \\ \hline \end{array}$$

7 Solve these multiplication problems:

a 4×3.221

b 5×6.78

c 8×4.916

8 Solve these division problems. Express any remainders as decimals:

a

$$4 \overline{) 16.56}$$

b

$$3 \overline{) 23.25}$$

c

$$4 \overline{) 35}$$

9 Solve these problems. Choose which operation you will use and show your working out:

a Jock buys 4 boxes of golf balls. Each box costs him \$55.99. How much does he spend in total?

b Lizzie, Daniel and Ky are all 1.67 m tall. What is their combined height?

c You order a hamburger costing \$4.95, a drink costing \$1.95 and fries costing \$1.85. What is the total cost of your order?

d You and 3 friends go out for pizza. The bill comes to \$25.60. What is your share if you split the bill evenly?

10 Multiply these numbers by 10, 100 or 1000:

	$\times 10$	$\times 100$	$\times 1000$
4			
3.7			
4.28			

11 Divide these numbers by 10, 100 or 1000:

	$\div 10$	$\div 100$	$\div 1000$
60			
32			
76.31			

Skills	Not yet	Kind of	Got it
• Adds decimals numbers with same or different number of decimal places			
• Subtracts decimals numbers with same or different number of decimal places			
• Multiplies decimals by single whole numbers			
• Divides decimals by single whole numbers			
• Multiplies decimals by 10, 100, 1000			
• Divides decimals by 10, 100, 1000			

1 Solve these addition and subtraction problems:

a $\frac{1}{4} + \frac{2}{4} = \frac{\boxed{3}}{\boxed{4}}$

c $\frac{5}{8} - \frac{3}{8} = \frac{\boxed{2}}{\boxed{8}}$

b $6\frac{1}{5} + 1\frac{3}{5} = \boxed{7}\frac{\boxed{4}}{\boxed{5}}$

d $3\frac{3}{12} - 1\frac{1}{12} = \boxed{2}\frac{\boxed{2}}{\boxed{12}}$

2 Solve these problems. Show your working out: *Answer strategies will vary.*

a Lisa has $\frac{3}{4}$ of a packet of chocolate. Bart also has $\frac{3}{4}$ of a packet. How much chocolate do they have in total?

$$\frac{3}{4} + \frac{3}{4} = \frac{6}{4} \text{ or } 1\frac{2}{4} \text{ or } 1\frac{1}{2}$$

b Niah has $4\frac{3}{4}$ packets of cookies and gives $2\frac{1}{4}$ to her friend. How many is she left with?

$$4 - 2 = 2$$

$$\frac{3}{4} - \frac{1}{4} = \frac{2}{4}$$

$$2\frac{2}{4} \text{ or } 2\frac{1}{2}$$

c $\frac{2}{4} + \frac{3}{8} =$

$$\frac{2}{4} = \frac{4}{8}$$

$$\frac{4}{8} + \frac{3}{8} = \frac{7}{8}$$

d Achmed spends $\frac{3}{4}$ of an hour on Live Mathletics on Monday. On Tuesday, he spends $\frac{1}{2}$ an hour. Write the amount of time he has spent as a fraction:

$$\frac{3}{4} + \frac{2}{4} = \frac{5}{4} \text{ or } 1\frac{1}{4}$$

What is this in minutes? 75 mins

3 Use repeated addition to multiply these fractions. Express your answer as an improper fraction and as a mixed numeral if necessary:

a $3 \times \frac{1}{6} = \frac{\boxed{1}}{\boxed{6}} + \frac{\boxed{1}}{\boxed{6}} + \frac{\boxed{1}}{\boxed{6}} = \frac{\boxed{3}}{\boxed{6}}$

b $2 \times \frac{5}{8} = \frac{\boxed{5}}{\boxed{8}} + \frac{\boxed{5}}{\boxed{8}} = \frac{\boxed{10}}{\boxed{8}} = \boxed{1}\frac{\boxed{2}}{\boxed{8}}$

c $3 \times \frac{3}{8} = \frac{\boxed{3}}{\boxed{8}} + \frac{\boxed{3}}{\boxed{8}} + \frac{\boxed{3}}{\boxed{8}} = \frac{\boxed{9}}{\boxed{8}} = \boxed{1}\frac{\boxed{1}}{\boxed{8}}$

d $4 \times \frac{5}{7} = \frac{\boxed{5}}{\boxed{7}} + \frac{\boxed{5}}{\boxed{7}} + \frac{\boxed{5}}{\boxed{7}} + \frac{\boxed{5}}{\boxed{7}} = \frac{\boxed{20}}{\boxed{7}} = \boxed{2}\frac{\boxed{6}}{\boxed{7}}$

4 Multiply these fractions. Express the answers as improper fractions:

a $3 \times \frac{3}{4}$

$$\frac{\boxed{3} \times \boxed{3}}{\boxed{4}} = \frac{\boxed{9}}{\boxed{4}}$$

b $3 \times \frac{2}{4}$

$$\frac{\boxed{3} \times \boxed{2}}{\boxed{4}} = \frac{\boxed{6}}{\boxed{4}}$$

c $5 \times \frac{3}{5}$

$$\frac{\boxed{5} \times \boxed{3}}{\boxed{5}} = \frac{\boxed{15}}{\boxed{5}}$$

d $2 \times \frac{3}{6}$

$$\frac{\boxed{2} \times \boxed{3}}{\boxed{6}} = \frac{\boxed{6}}{\boxed{6}}$$

5 Add these decimals:

$$\begin{array}{r} \text{a} \quad \quad 4 \quad 2 \quad . \quad 5 \\ + \quad 3 \quad 4 \quad . \quad 4 \\ \hline \quad 7 \quad 6 \quad . \quad 9 \\ \hline \end{array}$$

$$\begin{array}{r} \text{b} \quad \quad \quad \overset{1}{8} \quad \overset{1}{4} \quad . \quad 5 \\ + \quad \quad 3 \quad 7 \quad . \quad 6 \\ \hline \quad 1 \quad 2 \quad 2 \quad . \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} \text{c} \quad \quad 6 \quad \overset{1}{0} \quad . \quad 4 \quad 2 \\ + \quad 2 \quad 5 \quad . \quad 9 \quad 0 \\ \hline \quad 8 \quad 6 \quad . \quad 3 \quad 2 \\ \hline \end{array}$$

$$\begin{array}{r} \text{d} \quad \quad \quad 3 \quad . \quad \overset{1}{0} \quad 7 \quad 4 \\ + \quad \quad 9 \quad . \quad 2 \quad 6 \quad 2 \\ \hline \quad 1 \quad 2 \quad . \quad 3 \quad 3 \quad 6 \\ \hline \end{array}$$

$$\begin{array}{r} \text{e} \quad \quad 4 \quad . \quad 1 \quad 5 \\ + \quad 3 \quad . \quad 4 \quad 0 \\ \hline \quad 7 \quad . \quad 5 \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} \text{f} \quad \quad 7 \quad . \quad \overset{1}{0} \quad 4 \quad 2 \\ + \quad 1 \quad . \quad 8 \quad 7 \quad 0 \\ \hline \quad 8 \quad . \quad 9 \quad 1 \quad 2 \\ \hline \end{array}$$

6 Subtract these decimals:

$$\begin{array}{r} \text{a} \quad \quad 5 \quad 5 \quad . \quad 3 \\ - \quad 4 \quad 1 \quad . \quad 2 \\ \hline \quad 1 \quad 4 \quad . \quad 1 \\ \hline \end{array}$$

$$\begin{array}{r} \text{b} \quad \quad 5 \quad \overset{5}{\cancel{6}} \quad . \quad \overset{1}{3} \\ - \quad 2 \quad 4 \quad . \quad 6 \\ \hline \quad 3 \quad 1 \quad . \quad 7 \\ \hline \end{array}$$

$$\begin{array}{r} \text{c} \quad \quad \overset{4}{\cancel{5}} \quad \overset{10}{\cancel{1}} \quad . \quad \overset{15}{\cancel{6}} \quad \overset{1}{3} \\ - \quad 3 \quad 4 \quad . \quad 7 \quad 8 \\ \hline \quad 1 \quad 6 \quad . \quad 8 \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} \text{d} \quad \quad 6 \quad . \quad \overset{2}{\cancel{3}} \quad \overset{1}{5} \quad 4 \\ - \quad 4 \quad . \quad 0 \quad 6 \quad 0 \\ \hline \quad 2 \quad . \quad 2 \quad 9 \quad 4 \\ \hline \end{array}$$

$$\begin{array}{r} \text{e} \quad \quad \overset{2}{\cancel{3}} \quad . \quad \overset{10}{\cancel{1}} \quad \overset{1}{6} \quad 7 \\ - \quad 2 \quad . \quad 3 \quad 8 \quad 3 \\ \hline \quad 0 \quad . \quad 7 \quad 8 \quad 4 \\ \hline \end{array}$$

$$\begin{array}{r} \text{f} \quad \quad \overset{7}{\cancel{8}} \quad . \quad \overset{9}{\cancel{10}} \quad \overset{12}{\cancel{3}} \quad \overset{1}{1} \\ - \quad 7 \quad . \quad 1 \quad 7 \quad 4 \\ \hline \quad 0 \quad . \quad 8 \quad 5 \quad 7 \\ \hline \end{array}$$

7 Solve these multiplication problems:

a 4×3.221

$$\begin{array}{r} \quad \quad \quad 3 \quad . \quad 2 \quad 2 \quad 1 \\ \times \quad \quad \quad 4 \\ \hline \quad 1 \quad 2 \quad . \quad 8 \quad 8 \quad 4 \\ \hline \end{array}$$

b 5×6.78

$$\begin{array}{r} \quad \quad \quad \overset{3}{6} \quad . \quad \overset{4}{7} \quad 8 \\ \times \quad \quad \quad 5 \\ \hline \quad 3 \quad 3 \quad . \quad 9 \quad 0 \\ \hline \end{array}$$

c 8×4.916

$$\begin{array}{r} \quad \quad \quad \overset{7}{4} \quad . \quad \overset{1}{9} \quad \overset{4}{1} \quad 6 \\ \times \quad \quad \quad 8 \\ \hline \quad 3 \quad 9 \quad . \quad 3 \quad 2 \quad 8 \\ \hline \end{array}$$

8 Solve these division problems. Express any remainders as decimals:

a

$$\begin{array}{r} \quad \quad \quad 4 \quad . \quad 1 \quad 4 \\ 4 \overline{) 1 \quad 6 \quad . \quad 5 \quad \overset{1}{6}} \end{array}$$

b

$$\begin{array}{r} \quad \quad \quad 7 \quad . \quad 7 \quad 5 \\ 3 \overline{) 2 \quad 3 \quad . \quad \overset{2}{2} \quad \overset{1}{5}} \end{array}$$

c

$$\begin{array}{r} \quad \quad \quad 8 \quad . \quad 7 \quad 5 \\ 4 \overline{) 3 \quad 5 \quad . \quad \overset{3}{0} \quad \overset{2}{0}} \end{array}$$

9 Solve these problems. Choose which operation you will use and show your working out:

- a** Jock buys 4 boxes of golf balls. Each box costs him \$55.99. How much does he spend in total?

\$223.96

- b** Lizzie, Daniel and Ky are all 1.67 m tall. What is their combined height?

5.01 m

- c** You order a hamburger costing \$4.95, a drink costing \$1.95 and fries costing \$1.85. What is the total cost of your order?

\$8.75

- d** You and 3 friends go out for pizza. The bill comes to \$25.60. What is your share if you split the bill evenly?

\$6.40

Strategies will vary.

10 Multiply these numbers by 10, 100 or 1000:

	$\times 10$	$\times 100$	$\times 1000$
4	40	400	4000
3.7	37	370	3700
4.28	42.8	428	4280

11 Divide these numbers by 10, 100 or 1000:

	$\div 10$	$\div 100$	$\div 1000$
60	6	0.6	0.06
32	3.2	0.32	0.032
76.31	7.631	0.7631	0.07631

Skills	Not yet	Kind of	Got it
• Adds decimals numbers with same or different number of decimal places			
• Subtracts decimals numbers with same or different number of decimal places			
• Multiplies decimals by single whole numbers			
• Divides decimals by single whole numbers			
• Multiplies decimals by 10, 100, 1000			
• Divides decimals by 10, 100, 1000			

Series G – Fractions, Decimals and Percentages

Curriculum		Outcomes
National Curriculum	ACMNA125	Compare fractions with related denominators and locate and represent them on a number line
	ACMNA126	Solve problems involving addition and subtraction of fractions with the same or related denominators
	ACMNA127	Find a simple fraction of a quantity where the result is a whole number, with and without digital technologies
	ACMNA128	Add and subtract decimals, with and without digital technologies, and use estimation and rounding to check the reasonableness of answers
	ACMNA129	Multiply decimals by whole numbers and perform divisions by non-zero whole numbers where the results are terminating decimals, with and without digital technologies
	ACMNA130	Multiply and divide decimals by powers of 10
	ACMNA131	Make connections between equivalent fractions, decimals and percentage
	ACMNA132	Investigate and calculate percentage discounts of 10%, 25% and 50% on sale items, with and without digital technologies
NSW	MA3-7NA	Compares, orders and calculates with fractions, decimals and percentages
	MA3-1WM	Describes and represents mathematical situations in a variety of ways using mathematical terminology and some conventions
	MA3-2WM	Selects and applies appropriate problem-solving strategies, including the use of digital technologies, in undertaking investigations
	MA3-3WM	Gives a valid reason for supporting one possible solution over another
AusVELS	ACMNA125	Compare fractions with related denominators and locate and represent them on a number line
	ACMNA126	Solve problems involving addition and subtraction of fractions with the same or related denominators
	ACMNA127	Find a simple fraction of a quantity where the result is a whole number, with and without digital technologies
	ACMNA128	Add and subtract decimals, with and without digital technologies, and use estimation and rounding to check the reasonableness of answers
	ACMNA129	Multiply decimals by whole numbers and perform divisions by non-zero whole numbers where the results are terminating decimals, with and without digital technologies
	ACMNA130	Multiply and divide decimals by powers of 10
	ACMNA131	Make connections between equivalent fractions, decimals and percentage
	ACMNA132	Investigate and calculate percentage discounts of 10%, 25% and 50% on sale items, with and without digital technologies